

RustBelt: Securing the Foundations of the Rust Programming Language



Ralf Jung
Jacques-Henri Jourdan
Robbert Krebbers
Derek Dreyer
MPI-SWS & TU Delft

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ETH Zürich

Rust

Mozilla's replacement for C/C++

A safe & flexible systems programming language

- Modern strongly-typed PL:
 - First-class functions, polymorphism/generics
 - *Traits* \approx Type classes + associated types
- But with control over resource management (e.g., memory allocation and data layout)
- **Sound type system** with strong guarantees:
 - Type & memory safety; absence of data races



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- **Sound? type system** with strong guarantees:
 - Type & memory safety; absence of data races



Goal of ERC RustBelt project:

- **Prove the soundness** of Rust's type system in Coq!



The key challenge

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But this is not always true!

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- The safety of this is highly non-obvious because these libraries make use of **unsafe features!**

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- **Many Rust libraries permit mutation through aliased pointers**
- The safety of this is highly non-obvious because these libraries make use of **unsafe features!**

So why is any of this sound?

Introduction

Overview of Rust

RustBelt

Conclusion

```
let (snd, rcv) = channel();
join(
  move || { // First thread
    // Allocating [b] as Box<i32> (pointer to heap)
    let mut b = Box::new(0);
    *b = 1;

    // Transferring the ownership to the other thread...
    snd.send(b);

  },
  move || { // Second thread
    let b = rcv.recv().unwrap(); // ... that receives it
    println!("{}", *b);        // ... and uses it.
  });
```



```

let (snd, rcv) = channel();
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    let mut b = Box::new(0);
    *b = 1;

    // Transferring the ownership to the other thread...
    snd.send(b);
    *b = 2;    // Error: lost ownership of [b]
               // ==> Prevents data race
  },
  move || { // Second thread
    let b = rcv.recv().unwrap(); // ... that receives it
    println!("{}", *b);         // ... and uses it.
  });

```

Borrowing and lifetimes

```
let mut v = vec![1, 2, 3];
```

```
v[1] = 4;
```

```
v.push(6);  
println!("{:?}", v);
```

Borrowing and lifetimes

```
let mut v = vec![1, 2, 3];  
  
{ let mut inner_ptr = Vec::index_mut(&mut v, 1);  
  
    *inner_ptr = 4; }  
  
v.push(6);  
println!("{:?}", v);
```

Borrowing and lifetimes

```
let mut v = vec![1, 2, 3];

{ let mut inner_ptr = Vec::index_mut(&mut v, 1);
  // Error: can invalidate [inner_ptr]
  v.push(1);
  *inner_ptr = 4; }

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```


Borrowing and lifetimes

```
let mut v = vec![1, 2, 3];
```


```
{ let mut inner_ptr = Vec::index_mut(&mut v, 1);  
  // Error: can invalidate [inner_ptr]  
  v.push(1);  
  *inner_ptr = 4; }
```

```
v.push(6);  
println!("{:?}", v);
```

We temporarily lost ownership of vector v



We get back the full ownership of vector v



Borrowing and lifetimes

```
let mut
```

```
{ let
```

```
*inn
```

```
v.push
```

```
println!
```

Type of `index_mut`:

```
fn<'a> index_mut(&'a mut Vec<i32>, usize)  
    -> &'a mut i32
```

New pointer type: `&'a mut T`:

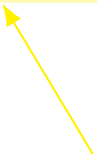
- **mutable borrowed** reference
- valid only for **lifetime** `'a`

Borrowing and lifetimes

```
let mut v = vec![1, 2, 3];
```

```
{ let mut inner_ptr = Vec::index_mut(&mut v, 1);  
  
  *inner_ptr = 4; }
```

```
v.push(6);  
println!("{:?}", v);
```



Lifetime 'a inferred by Rust

Shared borrowing

```
let mut x = 1;  
join (|| println!("{}", &x),  
      || println!("{}", &x));  
x = 2;
```


Shared borrowing

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let mut x = 1;  
join (|| println!("{}", &x),  
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x = 2;
```

`&x` creates a **shared borrow** of `x`

- Type: `&'a i32`
- Can be copied/shared
- Does not allow mutation

Summing up

- Rust's type system is based on **ownership**
- Three kinds of ownership:
 1. Full ownership: `Vec<T>` (vector), `Box<T>` (pointer to heap)
 2. **Mutable borrowed** reference: `&'a mut T`
 3. **Shared borrowed** reference: `&'a T`
- **Lifetimes** decide when borrows are valid

Interior mutability

What if we want **shared mutable data structures**?

Rust standard library provides types with **interior mutability**

- Allows mutation using only a shared reference `&'a T`
- Implemented in Rust **using unsafe features**
- Unsafety is claimed to be **safely encapsulated**
 - The library interface restricts what mutations are possible

Mutex

An example of Interior mutability

```
let m = Mutex::new(1); // m : Mutex<i32>

// We can mutate the integer
// *with a shared borrow* only
join (|| *(&m).lock().unwrap() += 1,
      || *(&m).lock().unwrap() += 1);

// Unique owner: no need to lock
println!("{}", m.into_inner().unwrap())
```

Mutex

An example of Interior mutability

```
let m
```

```
// We
```

```
// *w
```

```
join
```

```
// Un
```

```
print
```

A shared borrow **establishes a sharing protocol:**

- `&'a i32`

- \implies **Read-only**

- Safety: trivial

- `&'a Mutex<i32>`

- \implies Read-write **by taking the lock**

- Safety: ensured by proper synchronization

How do we know this all works?

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The λ_{Rust} type system

- Syntactic (built-in types)

$$\tau ::= \mathbf{bool} \mid \mathbf{int} \mid \mathbf{own}_n \tau \mid \&_{\mathbf{mut}}^{\kappa} \tau \mid \&_{\mathbf{shr}}^{\kappa} \tau \mid \Pi \bar{\tau} \mid \Sigma \bar{\tau} \mid \dots$$

- Typing context \mathbf{T} assigns types τ to paths p
- Typing individual instructions:

(Γ binds variables, \mathbf{E} and \mathbf{L} track lifetimes)

$$\Gamma \mid \mathbf{E}; \mathbf{L} \mid \mathbf{T}_1 \vdash S \dashv x. \mathbf{T}_2$$

- Typing whole functions: (\mathbf{K} tracks continuations)

$$\Gamma \mid \mathbf{E}; \mathbf{L} \mid \mathbf{K}, \mathbf{T} \vdash F$$

Some typing rules

$$\frac{\Gamma \mid \mathbf{E}; \mathbf{L} \vdash \kappa \text{ alive}}{\Gamma \mid \mathbf{E}; \mathbf{L} \mid p_1 \triangleleft \&_{\text{mut}}^{\kappa} \tau, p_2 \triangleleft \tau \vdash p_1 := p_2 \dashv p_1 \triangleleft \&_{\text{mut}}^{\kappa} \tau}$$

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$$\frac{\Gamma \mid \mathbf{E}; \mathbf{L} \mid \mathbf{T}_1 \vdash S \dashv x. \mathbf{T}_2 \quad \Gamma, x : \text{val} \mid \mathbf{E}; \mathbf{L} \mid \mathbf{K}; \mathbf{T}_2, \mathbf{T} \vdash F}{\Gamma \mid \mathbf{E}; \mathbf{L} \mid \mathbf{K}; \mathbf{T}_1, \mathbf{T} \vdash \text{let } x = S \text{ in } F}$$

Syntactic type safety

The standard “syntactic” approach to language safety is to prove a theorem like the following, via good old “progress and preservation”:

$$\mathbf{E; L \mid K, T} \vdash F \implies F \text{ is safe}$$

- **Problem:** This theorem does not help when unsafe code is used!
- **Solution:** A more semantic approach based on **logical relations**

The logical relation

- Define, for every type τ , an **ownership predicate**, where t is the owning thread's id and \bar{v} is the representation of τ :

$$\llbracket \tau \rrbracket.\text{own}(t, \bar{v})$$

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$$\begin{aligned} \llbracket \rho_1 \triangleleft \tau_1, \rho_2 \triangleleft \tau_2 \rrbracket(t) &:= \\ &\llbracket \tau_1 \rrbracket.\text{own}(t, [\rho_1]) * \llbracket \tau_2 \rrbracket.\text{own}(t, [\rho_2]) \end{aligned}$$

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- Lift to semantic typing judgments:

$$\begin{aligned} \mathbf{E}; \mathbf{L} \mid \mathbf{T}_1 \models S \equiv \mathbf{T}_2 &:= \\ \forall t. \{ \llbracket \mathbf{E} \rrbracket * \llbracket \mathbf{L} \rrbracket * \llbracket \mathbf{T}_1 \rrbracket(t) \} S \{ \llbracket \mathbf{E} \rrbracket * \llbracket \mathbf{L} \rrbracket * \llbracket \mathbf{T}_2 \rrbracket(t) \} \end{aligned}$$

Compatibility lemmas

To connect logical relation to type system,
we show **semantic versions** of all **syntactic typing rules**.

$$\frac{\Gamma \mid \mathbf{E}; \mathbf{L} \vdash \kappa \text{ alive}}{\Gamma \mid \mathbf{E}; \mathbf{L} \mid p_1 \triangleleft \&_{\text{mut}}^{\kappa} \tau, p_2 \triangleleft \tau \vdash p_1 := p_2 \dashv p_1 \triangleleft \&_{\text{mut}}^{\kappa} \tau}$$

$$\frac{\mathbf{E}; \mathbf{L} \mid \mathbf{T}_1 \vdash S \dashv x. \mathbf{T}_2 \quad \mathbf{E}; \mathbf{L} \mid \mathbf{K}; \mathbf{T}_2, \mathbf{T} \vdash F}{\mathbf{E}; \mathbf{L} \mid \mathbf{K}; \mathbf{T}_1, \mathbf{T} \vdash \text{let } x = S \text{ in } F}$$

Compatibility lemmas

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$$\frac{\Gamma \mid \mathbf{E}; \mathbf{L} \models_{\kappa} \text{alive}}{\Gamma \mid \mathbf{E}; \mathbf{L} \mid p_1 \triangleleft \&_{\text{mut}}^{\kappa} \tau, p_2 \triangleleft \tau \models p_1 := p_2 \equiv p_1 \triangleleft \&_{\text{mut}}^{\kappa} \tau}$$

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Type safety (revisited)

- From compatibility:

$$\mathbf{E}; \mathbf{L} \mid \mathbf{K}, \mathbf{T} \vdash F \dashv \mathbf{T}_2 \implies \mathbf{E}; \mathbf{L} \mid \mathbf{K}, \mathbf{T} \models F \dashv \mathbf{T}_2$$

- Finally, we show that the relation is **adequate**:

$$\mathbf{E}; \mathbf{L} \mid \mathbf{T}_1 \models F \dashv \mathbf{T}_2 \implies F \text{ is safe}$$

- Conclusion: **well-typed programs can't go wrong**
 - No data race, no memory error, ...

Type safety (semantic version)

The semantic approach provides a much stronger safety theorem than syntactic type safety:

- For well-typed code, $\mathbf{E}; \mathbf{L} \mid \mathbf{K}; \mathbf{T} \vdash F_{\text{safe}} \implies \mathbf{E}; \mathbf{L} \mid \mathbf{K}; \mathbf{T} \models F_{\text{safe}}$
- If unsafe features are used, manually prove $\mathbf{E}; \mathbf{L} \mid \mathbf{K}; \mathbf{T} \models F_{\text{unsafe}}$
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**The whole program is safe
if the “unsafe” pieces are safe.**

How do we define the logical interpretation of types?

Choosing the right logic

Rust type system has **ownership** + complex **sharing protocols**
in a **higher-order concurrent** setting

Choosing the right logic

Rust type system has **ownership** + complex **sharing protocols** in a **higher-order concurrent** setting

“Obvious” choice of a logic for interpreting Rust types:

Higher-order concurrent separation logic

Choosing the right logic

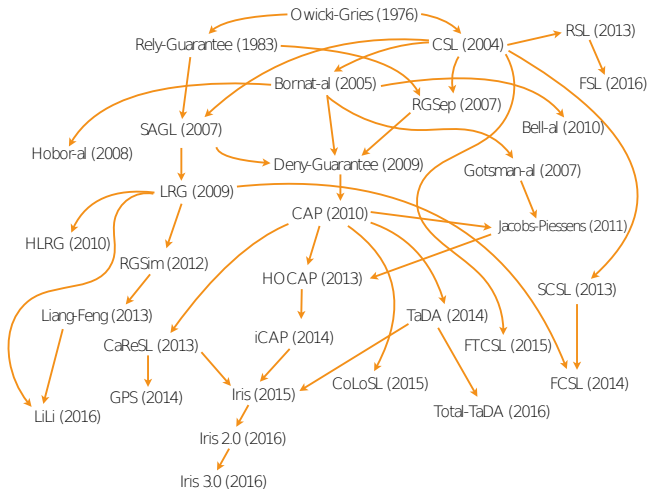
Rust type system has **ownership** + complex **sharing protocols** in a **higher-order concurrent** setting

“Obvious” choice of a logic for interpreting Rust types:

Higher-order concurrent separation logic

But which one?

A brief history of concurrent separation logic



Picture by Ilya Sergey

A brief history of concurrent separation logic

$$\frac{\Gamma, \Delta \mid \Phi \vdash \text{stable}(P) \quad \Gamma, \Delta \mid \Phi \vdash \forall y. \text{stable}(Q(y)) \quad \Gamma, \Delta \mid \Phi \vdash n \in C \quad \Gamma, \Delta \mid \Phi \vdash \forall x \in X. (x, f(x)) \in \overline{T(A)} \vee f(x) = x \quad \Gamma \mid \Phi \vdash \forall x \in X. (\Delta). \langle P * \otimes_{\alpha \in A} [\alpha]_{g(\alpha)}^n * \triangleright I(x) \rangle \quad c \langle Q(x) * \triangleright I(f(x)) \rangle \quad C \setminus \{n\}}{\Gamma \mid \Phi \vdash (\Delta). \langle P * \otimes_{\alpha \in A} [\alpha]_{g(\alpha)}^n * \text{region}(X, T, I, n) \rangle} \text{ATOMIC}$$

$$c$$

$$\langle \exists x. Q(x) * \text{region}(\{f(x)\}, T, I, n) \rangle^C$$

$$\frac{C \vdash \forall b \stackrel{\text{rely}}{\sqsupseteq}_{\pi} b_0. \langle \pi[b] * P \rangle \quad i \mapsto a \quad \langle x. \exists b' \stackrel{\text{guar}}{\sqsupseteq}_{\pi} b. \pi[b'] * Q \rangle}{C \vdash \left\{ \boxed{b_0}^n * \triangleright P \right\} \quad i \mapsto a \quad \left\{ x. \exists b'. \boxed{b'}^n * \right\}} \text{I1PnISI}$$

Use atomic rule

$$\frac{\lambda; \mathcal{A} \vdash \forall x \in X. \langle p_p \mid I(\mathbf{t}_a^\lambda(x)) * p(x) * [G]_a \rangle \quad C \quad \exists y \in Y. \langle q_p(x, y) \mid I(\mathbf{t}_a^\lambda(f(x))) * q(x, y) \rangle}{\lambda + 1; \mathcal{A} \vdash \forall x \in X. \langle p_p \mid \mathbf{t}_a^\lambda(x) * p(x) * [G]_a \rangle \quad C \quad \exists y \in Y. \langle q_p(x, y) \mid \mathbf{t}_a^\lambda(f(x)) * q(x, y) \rangle}$$

$$\Gamma \mid \Phi \vdash x \in X \quad \Gamma \mid \Phi \vdash \forall \alpha \in \text{Action}. \forall x \in \text{Sld} \times \text{Sld}. \text{up}(T(\alpha)(x))$$

$$\Gamma \mid \Phi \vdash A \text{ and } B \text{ are finite} \quad \Gamma \mid \Phi \vdash C \text{ is infinite}$$

$$\Gamma \mid \Phi \vdash \forall n \in C. P * \otimes_{\alpha \in A} [\alpha]_1^n \Rightarrow \triangleright I(n)(x)$$

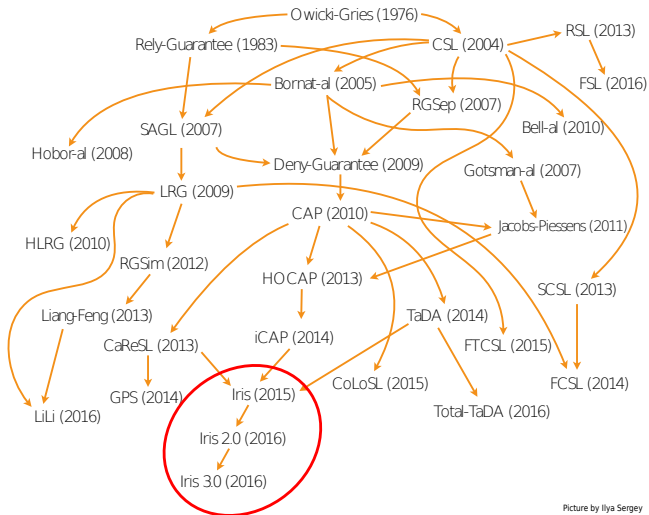
$$\frac{\Gamma \mid \Phi \vdash \forall n \in C. \forall s. \text{stable}(I(n)(s)) \quad \Gamma \mid \Phi \vdash A \cap B = \emptyset}{\Gamma \mid \Phi \vdash P \sqsubseteq^C \exists n \in C. \text{region}(X, T, I(n), n) * \otimes_{\alpha \in B} [\alpha]_1^n} \text{VALLOC}$$

Update region rule

$$\frac{\lambda; \mathcal{A} \vdash \forall x \in X. \left\langle p_p \mid I(\mathbf{t}_a^\lambda(x)) * p(x) \right\rangle \quad C \quad \exists y \in Y. \left\langle q_p(x, y) \mid \begin{array}{l} I(\mathbf{t}_a^\lambda(Q(x))) * q_1(x, y) \\ \vee I(\mathbf{t}_a^\lambda(x)) * q_2(x, y) \end{array} \right\rangle}{\forall x \in X. \left\langle p_p \mid \mathbf{t}_a^\lambda(x) * p(x) * a \Rightarrow \blacklozenge \right\rangle} \quad C$$

$$\lambda + 1; a : x \in X \rightsquigarrow Q(x), \mathcal{A} \vdash \exists y \in Y. \left\langle q_p(x, y) \mid \begin{array}{l} \exists z \in Q(x). \mathbf{t}_a^\lambda(z) * q_1(x, y) * a \Rightarrow (x, z) \\ \vee \mathbf{t}_a^\lambda(x) * q_2(x, y) * a \Rightarrow \blacklozenge \end{array} \right\rangle$$

A brief history of concurrent separation logic



Picture by Ilya Sergey

Iris

Iris is a higher-order concurrent separation logic framework that we have been developing since 2014 [POPL'15, ICFP'16, POPL'17, ESOP'17, ECOOP'17]

Distinguishing features of Iris:

- **Simple** foundation: Higher-order BI + a handful of modalities
- Rules for complex “sharing protocols” (which were built in as primitive in prior logics) are **derivable** in Iris
- Supports **impredicative invariants**, which arise when modeling recursive & generic types in Rust
- Excellent tactical support for **mechanization in Coq**

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- Excellent tactical support for **mechanization in Coq**

Iris is ideal for modeling Rust!

Ownership interpretations of simple types

$$\begin{aligned} & \llbracket \mathbf{bool} \rrbracket.\text{own}(t, \bar{v}) \\ & \quad := \\ & \bar{v} = [\mathbf{true}] \vee \bar{v} = [\mathbf{false}] \end{aligned}$$

$$\begin{aligned} & \llbracket \tau_1 \times \tau_2 \rrbracket.\text{own}(t, \bar{v}) \\ & \quad := \\ & \exists \bar{v}_1, \bar{v}_2. \bar{v} = \bar{v}_1 \# \bar{v}_2 * \llbracket \tau_1 \rrbracket.\text{own}(t, \bar{v}_1) * \llbracket \tau_2 \rrbracket.\text{own}(t, \bar{v}_2) \end{aligned}$$

Ownership interpretations of pointer types

$$\begin{aligned} & \llbracket \mathbf{own}_n \tau \rrbracket.\text{own}(t, \bar{v}) \\ & \quad := \\ \exists \ell. \bar{v} &= [\ell] * (\exists \bar{w}. \ell \mapsto \bar{w} * \triangleright \llbracket \tau \rrbracket.\text{own}(t, \bar{w})) * \dots \end{aligned}$$

$$\begin{aligned} & \llbracket \&_{\mathbf{mut}}^\kappa \tau \rrbracket.\text{own}(t, \bar{v}) \\ & \quad := \\ \exists \ell. \bar{v} &= [\ell] * \&^\kappa (\exists \bar{w}. \ell \mapsto \bar{w} * \llbracket \tau \rrbracket.\text{own}(t, \bar{w})) \end{aligned}$$

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What is this? Not your grandma's separation logic!

Lifetime logic: A custom logic derived within Iris

Traditionally, $P * Q$ splits ownership w.r.t. space

Let's allow **splitting ownership w.r.t. time!**

$$\triangleright P \quad \Rightarrow \quad \&^{\kappa} P * ([\dagger^{\kappa}] \Rightarrow \triangleright P)$$

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$\triangleright P$ can be transformed into...

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A *borrowed* part:

- access of P when κ is ongoing
- P must be *preserved* when κ ends

Lifetime logic: A custom logic derived within Iris

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Let's allow **splitting ownership w.r.t. time!**

$$\triangleright P \quad \Rightarrow \quad \&^{\kappa} P * \left([\dagger \kappa] \Rightarrow \triangleright P \right)$$

An *inheritance* part, that gives back P when κ is finished.

Lifetime tokens

How to witness that κ is alive?

We use a **lifetime token** $[\kappa]$

- **Left in deposit** when opening a borrow:

$$\&^{\kappa} P * [\kappa] \quad \Rightarrow \quad \triangleright P * (\triangleright P \Rightarrow \&^{\kappa} P * [\kappa])$$

- Needed to **terminate** κ :

$$[\kappa] \Rightarrow [\dagger\kappa]$$

Modeling shared references

As we've seen, each type T may have a different “sharing protocol” defining the semantics of $\&'a T$.

- E.g., $\&'a i32$ is read-only, whereas $\&'a \text{Mutex}\langle i32 \rangle$ grants mutable access to its contents once a lock is acquired

We model this by defining for each τ a “sharing predicate” $[[\tau]].shr$:

$$\begin{aligned} & [[\&_{shr}^{\kappa} \tau]].own(t, \bar{v}) \\ & \quad := \\ & \exists \ell. \bar{v} = [\ell] * [[\tau]].shr([[\kappa]], t, \ell) \end{aligned}$$

The sharing predicate is required to be **persistent**:

- I.e., freely duplicable, since in Rust $\&'a T$ is a **Copy** type

Modeling “thread-safety” of types

Some interior-mutable types are not thread-safe

- They support shared mutable access without atomics
- Examples: reference-counted pointer (`Rc<T>`), ...

Still, Rust **guarantees absence of data races**

- Ownership transfer between threads only allowed for some types
- $T : \text{Send} \iff T$ is thread-safe

In our model:

- Interpretations of types **may depend on the thread ID**
- $\llbracket T : \text{Send} \rrbracket \iff \llbracket T \rrbracket$ does not depend on TID

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What else is in the paper [POPL'18]

More details about the λ_{Rust} type system and “lifetime logic”

How to model essential Rust types featuring interior mutability

- `Cell<T>`, `RefCell<T>`, `Rc<T>`, `Arc<T>`, `Mutex<T>`, `RwLock<T>`

How to handle lifetime inclusion and subtyping

Still missing from RustBelt:

- Trait objects (existential types), weak memory, panics, ...

Conclusion

Logical relations are a great way to prove safety of a real language in an “extensible” way.

Advances in **separation logic** (as embodied in **Iris**) make this possible for even a language as sophisticated as Rust!

<http://plv.mpi-sws.org/rustbelt/>