

# Vulnerable Semantics of Solidity

**Sukyoung Ryu**

with PLRG@KAIST and friends

October 20, 2018

# Fortress, JavaScript, and Solidity

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# KAIST: SML and OCaml



## Links to other SML resources

Please feel free to send additional URLs that should be on this list to [smlnj-dev-list@mailman.cs.uchicago.edu](mailto:smlnj-dev-list@mailman.cs.uchicago.edu)

## SML Programming Resources

- [Concurrent ML](#)
- [sml\\_tk](#), a library for using the TK graphical interface, now updated to version 3.0
- Martin Erwig's [Functional Graph Library](#)
- Yi and Ryu's [SML/NJ exception analyzer](#)

# Harvard: Assembly, C, and Modula-3

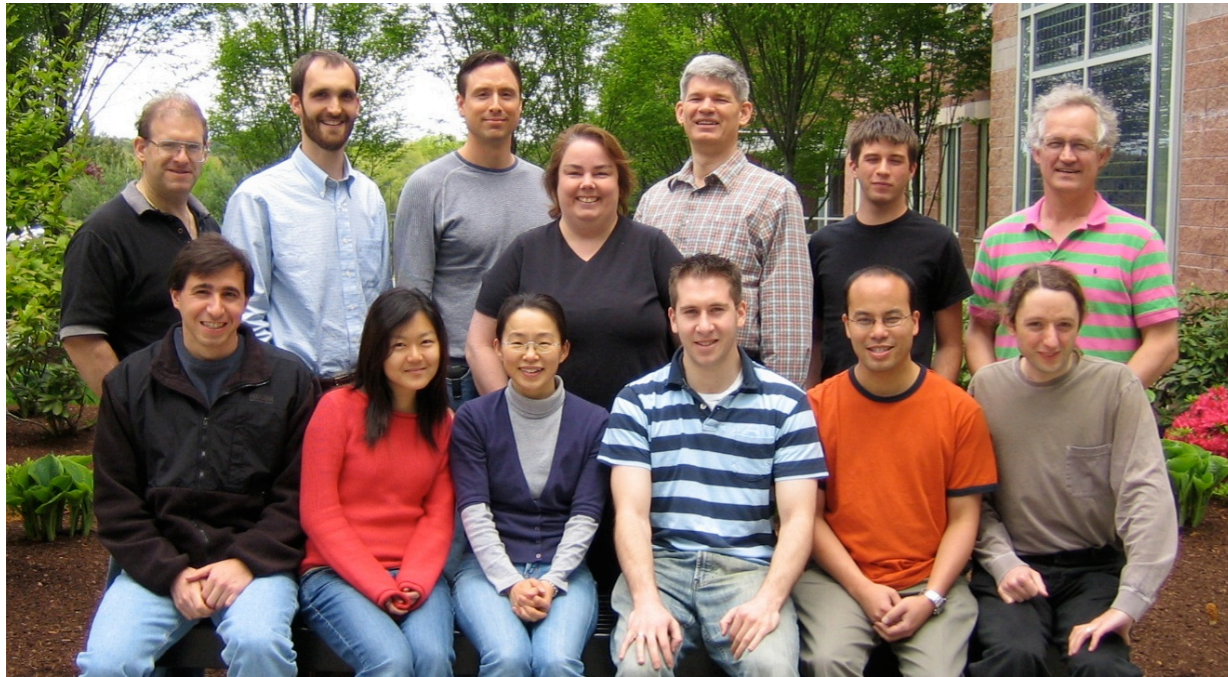


## Debugging Everywhere

The goal of the *Debugging Everywhere* project is to make debugging a cheap, ubiquitous service. We intend to begin by getting compilers to emit *Active Debugging Information*, which we expect will support multi-language, multi-platform debugging much more readily than older approaches like Dwarf or dbx ``stabs."

```
ldb Fib (stopped) > t
  0 <_print:2> (Mips/mjr.c:25,2) void _print(char *s = (0x1000008c) " ")
* 1 <fib:51+0x24> (Fib.java:23,32)
    void fib(Fib this = {int buffer = 10,
                        int[] a = {1, 1, 2, 3, 5, 8, 13, 21, 34, 55,
                                    0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
                        }, int n = 10)
  2 <main:3+0x18> (Fib.java:5,23) void main(String[] argv = {})
  3 <mAiN:end+0x1c> (mininub.c:7,9)
    int mAiN(int argc = 2, char **argv = 0x7fff7b24,
             char **envp = 0x7fff7b34)
```

# Sun Microsystems: Java and Scala



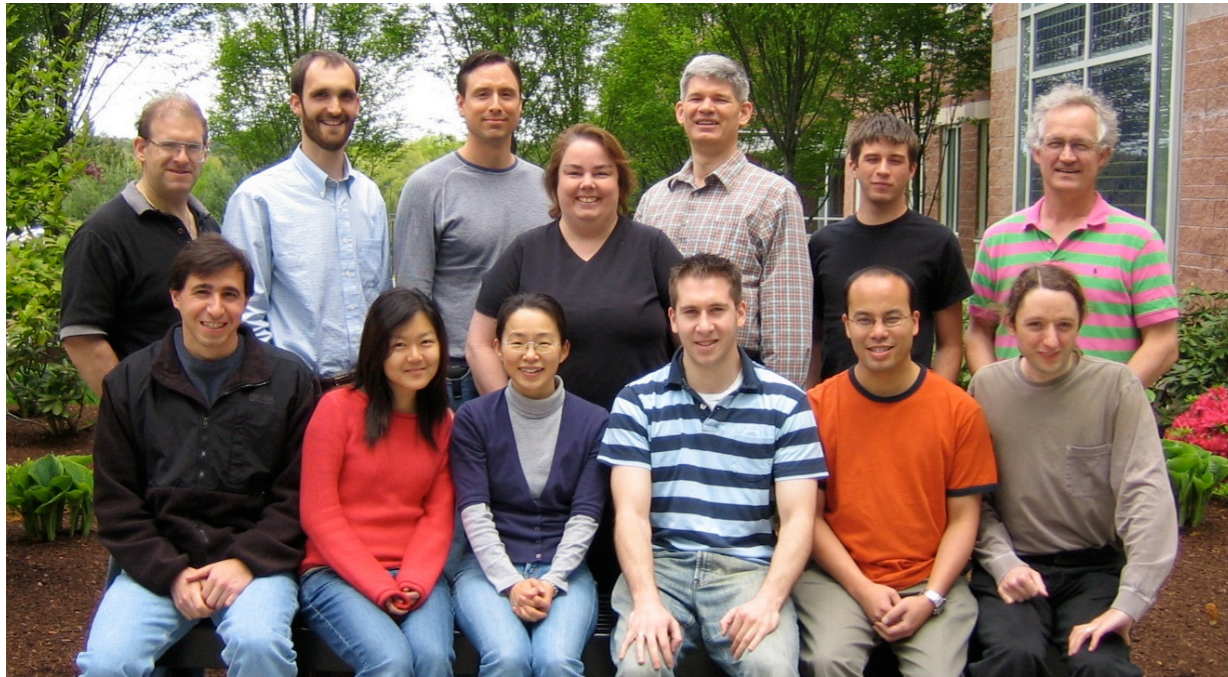
```

z: Vec := 0
r: Vec := x
p: Vec := r
ρ: Elt := rT r
for j ← seq(1: cgitmax) do
  q = Ap
  α =  $\frac{\rho}{p^T q}$ 
  z := z + αp
  r := r - αq
  ρ0 = ρ
  ρ := rT r
  β =  $\frac{\rho}{\rho_0}$ 
  p := r + βp
end
(z, ||x - Az||)
    
```

[sources / ProjectFortress / src / com / sun / fortress / parser](#)

Filename	Author	Revision	Modified	Log Entry
..				
 <a href="#">Compilation.rats</a>	chf	4575	over 4 years ago	Updated Copyright notices
 <a href="#">Declaration.rats</a>	chf	4575	over 4 years ago	Updated Copyright notices
 <a href="#">DelimitedExpr.rats</a>	sukyoungryu	4921	about 4 years ago	Revising
 <a href="#">Expression.rats</a>	Guy Steele	5051	almost 4 years ago	Completely redid assignment and ...
 <a href="#">Fortress.rats</a>	chf	4575	over 4 years ago	Updated Copyright notices

# Sun Microsystems: Fortress



$$v_{\text{norm}} = \underline{\underline{v / \|v\|}}$$

$$\sum_{\underline{k \leftarrow 1:n}} \underline{a_k} \underline{x^k}$$

$$C = \underline{A \cup B}$$

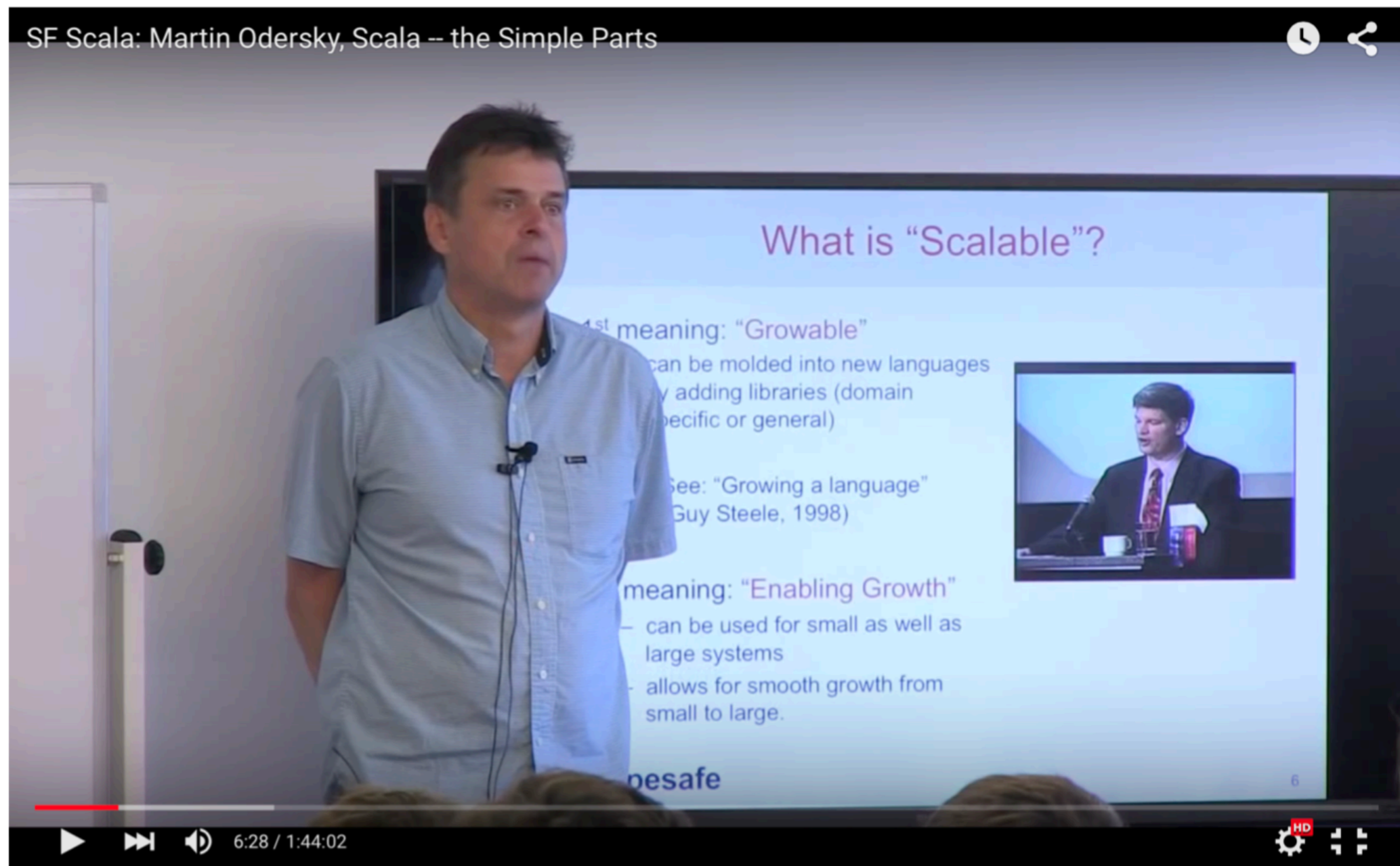
$$y = \underline{3x} \underline{\sin x} \underline{\cos 2x} \underline{\log \log x}$$

- A **multicore** language for **scientists and engineers**
- Run your **whiteboard in parallel!**
- “Growing a Language” [https://www.youtube.com/watch?v=\\_ahvzDzKdB0&t=10s](https://www.youtube.com/watch?v=_ahvzDzKdB0&t=10s)
  - ◆ Guy L. Steele Jr., keynote talk, OOPSLA 1998
  - ◆ Higher-Order and Symbolic Computation 12, 221-236 (1999)

# Sun Microsystems: Fortress

“It’s an absolute piece of beauty”

[https://www.youtube.com/watch?v=\\_ahvzDzKdB0](https://www.youtube.com/watch?v=_ahvzDzKdB0)



# Language *Manipulation*: Fortress

- Specification
- Parsing
- Static checking
- Compilation / Interpretation
- Testing
- Analysis
- Verification



# Fortress as a Language Designer

- Development from scratch
- Language evolves to experiment with new features
- Constant changes in spec., parsing, checking, ...
- Language development by 3 teams in tandem:
  - ◆ Specification team
  - ◆ Implementation team
  - ◆ Library team

# Fortress as a Language Designer

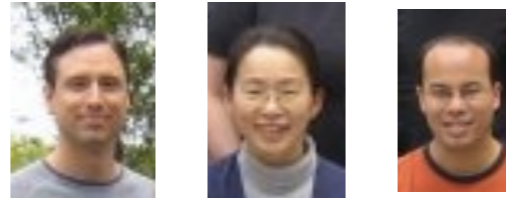
- Specification team



- ◆ Formal concrete grammar in EBNF
- ◆ Informal description in prose
- ◆ Examples & formal calculi

# Fortress as a Language Designer

## ■ Specification team



- ◆ Formal concrete grammar in EBNF
- ◆ Informal description in prose
- ◆ Examples & formal calculi

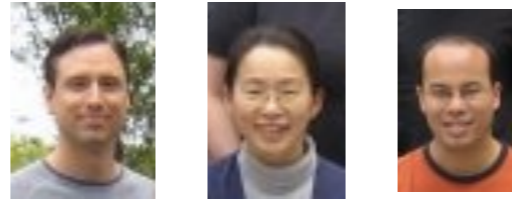
## ■ Library team



- ◆ Adventurous library in unimplemented Fortress features

# Fortress as a Language Designer

## ■ Specification team



- ◆ Formal concrete grammar in EBNF
- ◆ Informal description in prose
- ◆ Examples & formal calculi

## ■ Library team



- ◆ Adventurous library in unimplemented Fortress features

## ■ Implementation team



- ◆ Implementation extension
- ◆ Regression tests & new feature tests

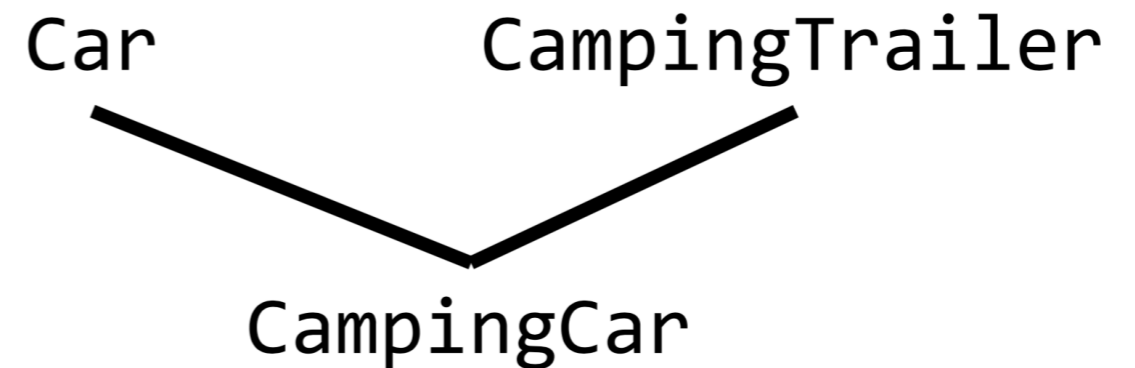
# Language *Manipulation*: Fortress

- Specification: automatic extraction/test of examples
- Parsing: automatic generation of parsers & ASTs
- Static checking: parallel development
- Compilation / Interpretation: cross validation
- Testing
- Analysis
- Verification
  - ◆ FFMM (Featherweight Fortress with Multiple Dispatch and Multiple Inheritance): 3,000 LOC (Coq)

# Fortress: Symmetric Multiple Dispatch

- Method overloading
  - ◆ Multiple method declarations of the same name
- Symmetric multiple dispatch
  - ◆ Selection of a method declaration at run time using all the arguments equally
- Overloading rules
  - ◆ Static rejection of ambiguous method declarations
  - ◆ No ambiguous nor undefined method call at run time!

# Fortress: Symmetric Multiple Dispatch



```
collide(c: Car, cc: CampingCar): Int = _
```

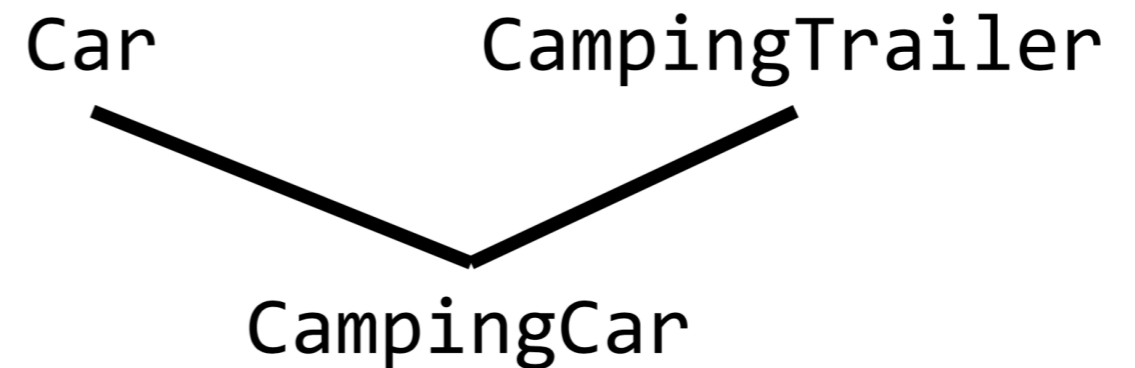
```
collide(cc: CampingCar, c: Car): Int = _
```

```
cc1: CampingCar = CampingCar()
```

```
cc2: CampingCar = CampingCar()
```

```
collide(cc1, cc2)
```

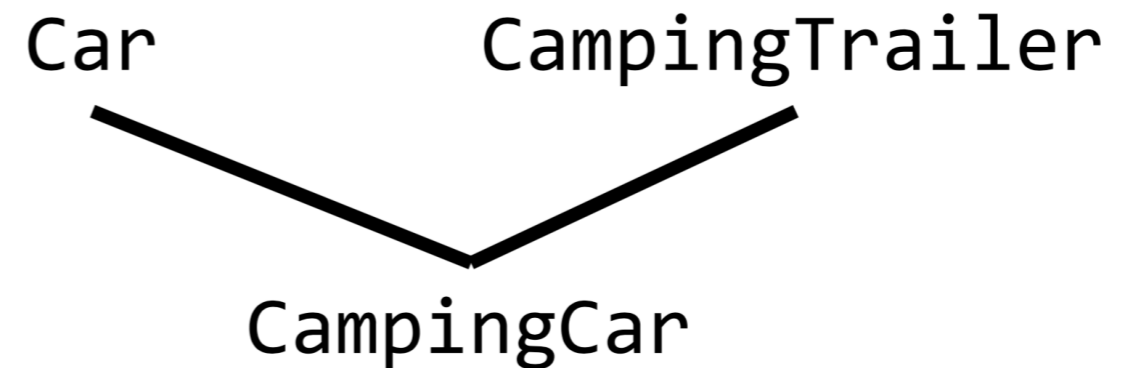
# Fortress: Symmetric Multiple Dispatch



```
collide(c: Car, cc: CampingCar): Int = _  
collide(cc: CampingCar, c: Car): Int = _  
collide(cc: CampingCar, c: CampingCar): Int = _  
cc1: CampingCar = CampingCar()  
cc2: CampingCar = CampingCar()  
collide(cc1, cc2)
```



# Fortress: Symmetric Multiple Dispatch



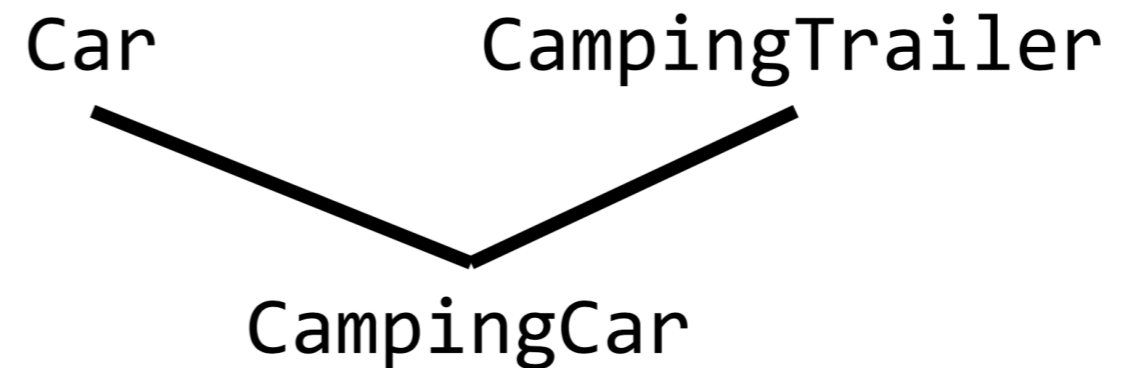
```
sort[P <: Car](x: List[P]): SortedList[P] = _
```

```
sort[P <: CampingTrailer](x: List[P]): SortedList[P] = _
```

```
l: List[CampingCar] = List(CampingCar())
```

```
sort(cc)
```

# Fortress: Symmetric Multiple Dispatch



```
sort[P <: Car](x: List[P]): SortedList[P] = _  
sort[P <: CampingTrailer](x: List[P]): SortedList[P] = _  
sort[P <: CampingCar](x: List[P]): SortedList[P] = _  
l: List[CampingCar] = List(CampingCar())  
sort(cc)
```

# Fortress: Symmetric Multiple Dispatch with Parametric Polymorphism

## Type Checking Modular Multiple Dispatch with Parametric Polymorphism and Multiple Inheritance

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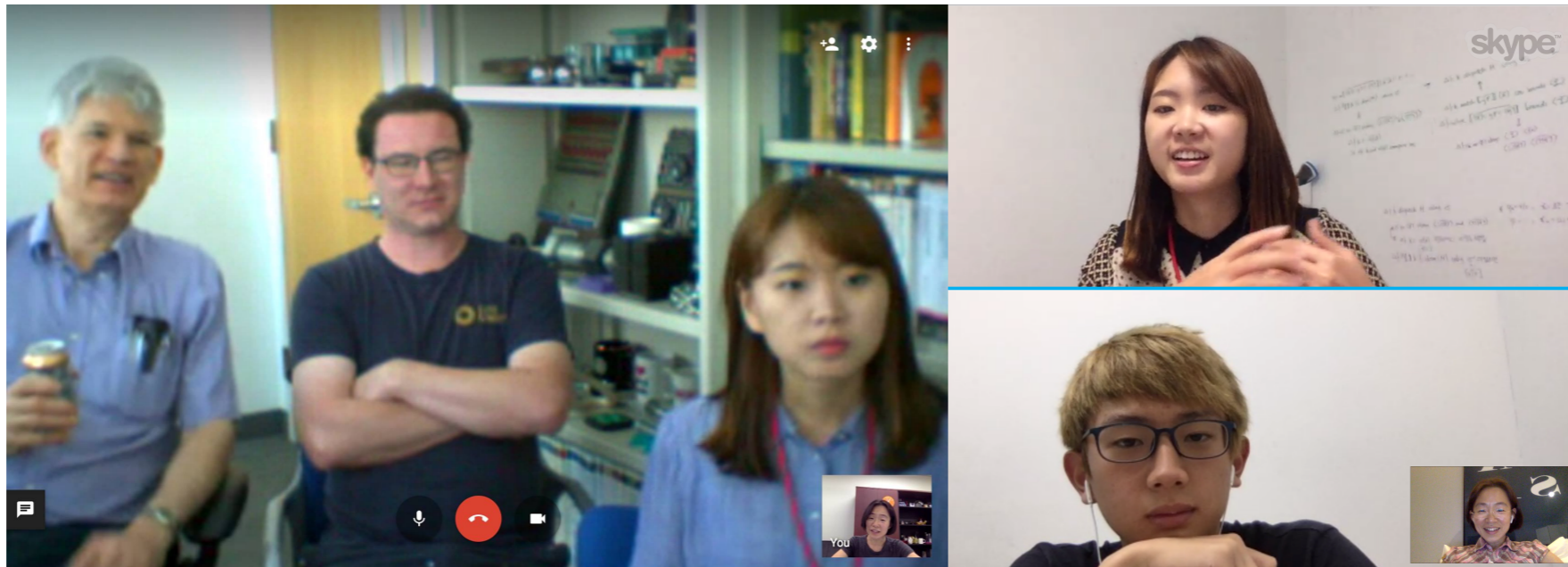
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Guy L. Steele Jr.  
Oracle Labs  
guy.steele@oracle.com

- OOPSLA'11
- **No** variance, **No** dynamic dispatch algorithm
- **No** type soundness proof

# Fortress: Symmetric Multiple Dispatch with Polymorphism and Variance





# Fortress: Symmetric Multiple Dispatch with Polymorphism and Variance

PROVED

## Polymorphic Symmetric Multiple Dispatch with Variance

GYUNGHEE PARK, Oracle Labs and KAIST

JAEMIN HONG, KAIST

GUY L. STEELE JR., Oracle Labs

SUKYOUNG RYU, KAIST

- POPL'19
- Yes variance, Yes dynamic dispatch algorithm
- Yes type soundness proof



# Fortress: Symmetric Multiple Dispatch with Polymorphism and Variance

PROVED

Program	$\Pi ::= \bar{\psi}, e$
Class declaration	$\psi ::= \text{trait } T[\bar{V} \bar{\beta}] <: \{\bar{t}\} \bar{\mu} \text{ end} \mid \text{object } O[\bar{\beta}](\bar{x}:\bar{\tau}) <: \{\bar{t}\} \bar{\mu} \text{ end}$
Method definition	$\mu ::= m[\bar{\kappa}](\bar{x}:\bar{\tau}): \tau = e$
Class type parameter binding	$\beta ::= P <: \{\bar{\tau}\}$
Method type parameter binding	$\kappa ::= \{\bar{\tau}\} <: P <: \{\bar{\tau}\}$
Variance mark	$V ::= + \mid - \mid =$
Expression	$e ::= z \mid ((\bar{x}:\bar{\tau}): \tau \Rightarrow e) \mid e@(\bar{e}) \mid O[\bar{\tau}](\bar{e}) \mid e.m(\bar{e})$
Bindable variable	$z ::= x \mid \text{self}$
Type	$\tau ::= P \mid c \mid (\bar{\tau}) \mid (\tau \rightarrow \tau) \mid \text{Any}$
Constructed type	$c ::= t \mid O[\bar{\tau}]$
Trait type	$t ::= T[\bar{\tau}]$

# Fortress: Symmetric Multiple Dispatch with Polymorphism and Variance

**PROVED**

Well-formed programs:  $\vdash \Pi : g$

$$\frac{\Pi = \overline{\psi}, e \quad \text{distinct}(\overline{\text{name}(\psi)}) \quad \Delta = \{\overline{\psi}\} \quad \overline{\Delta} \vdash \overline{\psi} \text{ ok} \quad \Delta; \bullet \vdash e : (-, g)}{\vdash \Pi : g} \text{ [T-PROGRAM]}$$

Well-formed trait and object declarations:  $\overline{\Delta} \vdash \overline{\psi} \text{ ok}$

$$\frac{\begin{array}{l} \Delta' = \Delta \cup \{\overline{\{ \langle P \rangle : \{ \overline{\xi} \}} \}} \quad \text{distinct}(\overline{P}) \quad \overline{\overline{\Delta'}} \vdash \overline{\xi} \text{ ok} \quad \overline{\Delta'} \vdash t \text{ ok} \\ \overline{\{ \overline{J} \}} = \text{properAncestors}(\Delta', T[\overline{P}]) \quad \overline{\Delta'}; \overline{J} \vdash J_i \text{ and } J_j \text{ ancestors ok} \\ \overline{T} \neq \text{name}(J) \quad \overline{\Delta'}; \text{self}:T[\overline{P}]; \overline{V} \overline{P} \vdash \mu \text{ ok} \quad \{ \overline{d} \} = \text{allVisible}(\Delta', T[\overline{P}]) \\ \overline{\Delta'} \vdash d_i \text{ not duplicate of } d_j^{1 \leq i < j \leq \#(\overline{d})} \quad \overline{\Delta'} \vdash d_i \text{ meet } d_j \text{ wrt } \{ \overline{d} \} \text{ ok} \\ \overline{\Delta'} \vdash d_i \text{ return type wrt } d_j \text{ ok}^{1 \leq i < j \leq \#(\overline{d})} \quad \overline{\Delta'} \vdash d_j \text{ return type wrt } d_i \text{ ok}^{1 \leq i < j \leq \#(\overline{d})} \end{array}}{\Delta \vdash \text{trait } T[\overline{V} \overline{P} \langle: \{ \overline{\xi} \}] \langle: \{ \overline{t} \}] \overline{\mu} \text{ end ok}} \text{ [D-TRAIT]}$$

$$\frac{\begin{array}{l} \Delta' = \Delta \cup \{\overline{\{ \langle P \rangle : \{ \overline{\xi} \}} \}} \quad \text{distinct}(\overline{P}) \quad \overline{\overline{\Delta'}} \vdash \overline{\xi} \text{ ok} \quad \overline{\Delta'} \vdash t \text{ ok} \\ \overline{\{ \overline{J} \}} = \text{properAncestors}(\Delta', O[\overline{P}]) \quad \overline{\Delta'}; \overline{J} \vdash J_i \text{ and } J_j \text{ ancestors ok} \\ \overline{\Delta'}; \text{self}:O[\overline{P}], \overline{x}:\overline{\tau}; \overline{=} \overline{P} \vdash \mu \text{ ok} \quad \{ \overline{d} \} = \text{allVisible}(\Delta', O[\overline{P}]) \\ \overline{\Delta'} \vdash d_i \text{ not duplicate of } d_j^{1 \leq i < j \leq \#(\overline{d})} \quad \overline{\Delta'} \vdash d_i \text{ meet } d_j \text{ wrt } \{ \overline{d} \} \text{ ok} \\ \overline{\Delta'} \vdash d_i \text{ return type wrt } d_j \text{ ok}^{1 \leq i < j \leq \#(\overline{d})} \quad \overline{\Delta'} \vdash d_j \text{ return type wrt } d_i \text{ ok}^{1 \leq i < j \leq \#(\overline{d})} \\ \overline{\Delta'} \vdash \tau \text{ ok} \quad \text{distinct}(\overline{x}) \end{array}}{\Delta \vdash \text{object } O[\overline{P} \langle: \{ \overline{\xi} \}](\overline{x}:\overline{\tau}) \langle: \{ \overline{t} \}] \overline{\mu} \text{ end ok}} \text{ [D-OBJECT]}$$

Well-formed method declarations:  $\Delta; \Gamma; \overline{V} \overline{P} \vdash \mu \text{ ok}$

$$\frac{\begin{array}{l} \Delta \vdash [\overline{\{ \overline{\xi} \}} \langle: \overline{Q} \langle: \{ \overline{\xi} \}}] \text{ ok} \quad \Delta' = \Delta \cup \{\overline{\{ \overline{\xi} \}} \langle: \overline{Q} \langle: \{ \overline{\xi} \}} \} \quad \overline{\overline{\Delta'}} \vdash \overline{\xi} \text{ ok} \quad \overline{\Delta'} \vdash \overline{\xi} \text{ ok} \\ \text{distinct}(\overline{x}) \quad \overline{\Delta'} \vdash \tau \text{ ok} \quad \Delta' \vdash \omega \text{ ok} \quad \Delta'; \Gamma, \overline{x}:\overline{\tau} \vdash e : (-, \rho) \quad \Delta' \vdash \rho \langle: \omega \\ \text{distinct}(\overline{P}, \overline{Q}) \quad (\overline{V} =) \vee (\forall \mathcal{T}. ((\overline{\tau}) \rightarrow \omega) \neq \mathcal{T}[P]) \vee (\overline{\Delta} \vdash \mathcal{T} \text{ variance } V)) \end{array}}{\Delta; \Gamma; \overline{V} \overline{P} \vdash m[\overline{\{ \overline{\xi} \}} \langle: \overline{Q} \langle: \{ \overline{\xi} \}](\overline{x}:\overline{\tau}): \omega = e \text{ ok}} \text{ [D-METHOD]}$$

Fig. 3. Well-formed programs, class declarations, and method declarations

# Fortress: Symmetric Multiple Dispatch with Polymorphism and Variance

**PROVED**

Well-formed programs:  $\vdash \Pi : g$

$$\frac{\Pi = \bar{\psi}, e \quad \text{distinct}(\text{name}(\bar{\psi})) \quad \Delta = \{\bar{\psi}\} \quad \underline{\Delta} \vdash \bar{\psi} \text{ ok} \quad \Delta; \bullet \vdash e : (-, g)}{\vdash \Pi : g} \text{ [T-PROGRAM]}$$

Well-formed trait and object declarations:  $\Delta \vdash \psi \text{ ok}$

$$\frac{\begin{array}{l} \Delta' = \Delta \cup \{\{\} <: P <: \{\bar{\xi}\}\} \quad \text{distinct}(\bar{P}) \quad \underline{\Delta'} \vdash \bar{\xi} \text{ ok} \quad \underline{\Delta'} \vdash t \text{ ok} \\ \{\bar{J}\} = \text{properAncestors}(\Delta', T[\bar{P}]) \quad \underline{\Delta'}; \bar{J} \vdash J_i \text{ and } J_j \text{ ancestors ok} \\ \underline{T} \neq \text{name}(J) \quad \underline{\Delta'}; \text{self}: T[\bar{P}]; \bar{V} \bar{P} \vdash \mu \text{ ok} \quad \{\bar{d}\} = \text{allVisible}(\Delta', T[\bar{P}]) \\ \underline{\Delta'} \vdash d_i \text{ not duplicate of } d_j \quad \underline{\Delta'} \vdash d_i \text{ meet } d_j \text{ wrt } \{\bar{d}\} \text{ ok} \\ \underline{\Delta'} \vdash d_i \text{ return type wrt } d_j \text{ ok} \quad \underline{\Delta'} \vdash d_j \text{ return type wrt } d_i \text{ ok} \end{array}}{\Delta \vdash \text{trait } T[\bar{V} P <: \{\bar{\xi}\}] <: \{\bar{t}\} \bar{\mu} \text{ end ok}} \text{ [D-TRAIT]}$$

$$\frac{\begin{array}{l} \Delta' = \Delta \cup \{\{\} <: P <: \{\bar{\xi}\}\} \quad \text{distinct}(\bar{P}) \quad \underline{\Delta'} \vdash \bar{\xi} \text{ ok} \quad \underline{\Delta'} \vdash t \text{ ok} \\ \{\bar{J}\} = \text{properAncestors}(\Delta', O[\bar{P}]) \quad \underline{\Delta'}; \bar{J} \vdash J_i \text{ and } J_j \text{ ancestors ok} \\ \underline{\Delta'}; \text{self}: O[\bar{P}], \bar{x}: \bar{\tau}; = \bar{P} \vdash \mu \text{ ok} \quad \{\bar{d}\} = \text{allVisible}(\Delta', O[\bar{P}]) \\ \underline{\Delta'} \vdash d_i \text{ not duplicate of } d_j \quad \underline{\Delta'} \vdash d_i \text{ meet } d_j \text{ wrt } \{\bar{d}\} \text{ ok} \\ \underline{\Delta'} \vdash d_i \text{ return type wrt } d_j \text{ ok} \quad \underline{\Delta'} \vdash d_j \text{ return type wrt } d_i \text{ ok} \\ \underline{\Delta'} \vdash \tau \text{ ok} \quad \text{distinct}(\bar{x}) \end{array}}{\Delta \vdash \text{object } O[\bar{P} <: \{\bar{\xi}\}](\bar{x}: \bar{\tau}) <: \{\bar{t}\} \bar{\mu} \text{ end ok}} \text{ [D-OBJECT]}$$

Well-formed method declarations:  $\Delta; \Gamma; \bar{V} \bar{P} \vdash \mu \text{ ok}$

$$\frac{\begin{array}{l} \Delta \vdash [\{\bar{\zeta}\} <: Q <: \{\bar{\xi}\}] \text{ ok} \quad \Delta' = \Delta \cup \{\{\bar{\zeta}\} <: Q <: \{\bar{\xi}\}\} \quad \underline{\Delta'} \vdash \bar{\zeta} \text{ ok} \quad \underline{\Delta'} \vdash \bar{\xi} \text{ ok} \\ \text{distinct}(\bar{x}) \quad \underline{\Delta'} \vdash \tau \text{ ok} \quad \Delta' \vdash \omega \text{ ok} \quad \Delta'; \Gamma, \bar{x}: \bar{\tau} \vdash e : (-, \rho) \quad \Delta' \vdash \rho <: \omega \\ \text{distinct}(\bar{P}, \bar{Q}) \quad (\bar{V} =) \vee (\forall \mathcal{T}. ((\bar{\tau} \rightarrow \omega) \neq \mathcal{T}[P]) \vee (\Delta \vdash \mathcal{T} \text{ variance } V)) \end{array}}{\Delta; \Gamma; \bar{V} \bar{P} \vdash m[\{\bar{\zeta}\} <: Q <: \{\bar{\xi}\}](\bar{x}: \bar{\tau}): \omega = e \text{ ok}} \text{ [D-METHOD]}$$

Fig. 3. Well-formed programs, class declarations, and method declarations

Well-formed ancestors:  $\Delta; \bar{J} \vdash J$  and  $J$  ancestors ok

$$\frac{T \neq T'}{\Delta; \bar{J} \vdash T[\bar{\alpha}] \text{ and } T'[\bar{\eta}] \text{ ancestors ok}} \text{ [ANC-DIFF-TRAIT]}$$

$$\frac{T[\bar{\gamma}] \in \{\bar{J}\} \quad \Delta \vdash T[\bar{\gamma}] <: T[\bar{\alpha}] \quad \Delta \vdash T[\bar{\gamma}] <: T[\bar{\eta}]}{\Delta; \bar{J} \vdash T[\bar{\alpha}] \text{ and } T[\bar{\eta}] \text{ ancestors ok}} \text{ [ANC-SAME-TRAIT]}$$

Well-formed type parameter bindings:  $\Delta \vdash [\bar{K}] \text{ ok}$

$$\Delta \vdash [] \text{ ok} \text{ [BINDING-EMPTY]}$$

$$\frac{\begin{array}{l} FV(\bar{\chi}') \subseteq \text{parameters}(\Delta) \cup \{\bar{P}\} \quad FV(\bar{\eta}') \subseteq \text{parameters}(\Delta) \\ \Delta \vdash \sqcup \{\bar{\chi}'\} <: \sqcap \{\bar{\eta}'\} \quad \Delta \vdash [\{\bar{\chi}\} <: P <: \{\bar{\eta}\}] \text{ ok} \end{array}}{\Delta \vdash [\{\bar{\chi}\} <: P <: \{\bar{\eta}\}, \{\bar{\chi}'\} <: P' <: \{\bar{\eta}'\}] \text{ ok}} \text{ [BINDING-STEP]}$$

Fig. 4. Well-formed ancestors and type parameter bindings



# Fortress: Symmetric Multiple Dispatch with Polymorphism and Variance

**PROVED**

Well-formed programs:  $\vdash \Pi : g$

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Well-formed trait and object declarations:

$$\frac{\Delta' = \Delta \cup \{\{\} <: P <: \{\bar{\xi}\}\} \quad \text{disti} \quad \{\bar{J}\} = \text{properAncestors}(\Delta', T[\bar{P}]) \quad \bar{L} \quad \bar{T} \neq \text{name}(J) \quad \underline{\Delta'}; \text{self}: T[\bar{P}]; \bar{V} \bar{P}}{\Delta' \vdash d_i \text{ not duplicate of } d_j \quad \Delta' \vdash d_i \text{ return type wrt } d_j \text{ ok} \quad \Delta \vdash \text{trait } T[\bar{V} P <: \{\bar{\xi}\}]}$$

$$\frac{\Delta' = \Delta \cup \{\{\} <: P <: \{\bar{\xi}\}\} \quad \text{distin} \quad \{\bar{J}\} = \text{properAncestors}(\Delta', O[\bar{P}]) \quad \bar{\Delta}' \quad \underline{\Delta'}; \text{self}: O[\bar{P}], \bar{x}: \bar{\tau}; = \bar{P} \vdash \mu \text{ ok}}{\Delta' \vdash d_i \text{ not duplicate of } d_j \quad \Delta' \vdash d_i \text{ return type wrt } d_j \text{ ok} \quad \Delta \vdash \text{object } O[\bar{P} <: \{\bar{\xi}\}]}$$

Well-formed method declarations:  $\Delta; \Gamma; \bar{V} \bar{P} \vdash$

$$\frac{\Delta \vdash [\{\bar{\xi}\} <: Q <: \{\bar{\xi}\}] \text{ ok} \quad \Delta' = \Delta \cup \{\{\bar{\xi}\} <: \{\bar{\xi}\}\} \quad \text{distinct}(\bar{x}) \quad \underline{\Delta'} \vdash \tau \text{ ok} \quad \Delta' \vdash \omega \text{ ok} \quad \text{distinct}(\bar{P}, \bar{Q}) \quad (\bar{V} =) \vee (\forall \mathcal{T}. ((\bar{\tau} \rightarrow \omega) \neq \mathcal{T}[P]) \vee (\Delta \vdash \mathcal{T} \text{ variance } V))}{\Delta; \Gamma; \bar{V} \bar{P} \vdash m[\{\bar{\xi}\} <: Q <: \{\bar{\xi}\}](\bar{x}: \bar{\tau}): \omega = e \text{ ok}} \text{ [D-METHOD]}$$

Fig. 3. Well-formed programs, class declarations, and method declarations

Well-formed ancestors:  $\Delta; \bar{J} \vdash J$  and  $J$  ancestors ok

$$\frac{T \neq T'}{\Delta; \bar{J} \vdash T[\bar{\alpha}] \text{ and } T'[\bar{\eta}] \text{ ancestors ok}} \text{ [ANC-DIFF-TRAIT]}$$

$$\frac{T[\bar{\gamma}] \in \{\bar{J}\} \quad \Delta \vdash T[\bar{\gamma}] <: T[\bar{\alpha}] \quad \Delta \vdash T[\bar{\gamma}] <: T[\bar{\eta}] \quad \text{nd } T[\bar{\eta}] \text{ ancestors ok}}{\Delta \vdash T[\bar{\gamma}] \text{ ok}} \text{ [ANC-SAME-TRAIT]}$$

$$\frac{\text{No Duplicates Rule: } \Delta \vdash d \text{ not duplicate of } d \quad \text{Meet Rule: } \Delta \vdash d \text{ meet } d' \text{ wrt } \{\bar{d}\} \text{ ok}}{\Delta \vdash d \text{ not duplicate of } d' \quad \Delta \vdash d \text{ meet } d' \text{ wrt } \_ \text{ ok}} \text{ [NO-DUP-TRIV]}$$

$$\frac{\text{Meet Rule: } \Delta \vdash d \text{ meet } d' \text{ wrt } \_ \text{ ok} \quad \Delta \vdash (\text{dom}(d) \cap \text{dom}(d')) \sqsubseteq \exists [\_]\text{Bottom}}{\Delta \vdash d \text{ meet } d' \text{ wrt } \_ \text{ ok} \quad \Delta \vdash \text{dom}(d) \sqsubseteq \text{dom}(d')} \text{ [MEET-EXCL]}$$

$$\frac{\Delta \vdash d \text{ meet } d' \text{ wrt } \_ \text{ ok} \quad \Delta \vdash \text{dom}(d) \sqsubseteq \text{dom}(d')}{\Delta \vdash d \text{ meet } d' \text{ wrt } \_ \text{ ok} \quad \Delta \vdash \text{dom}(d') \sqsubseteq \text{dom}(d)} \text{ [MEET-LESS]}$$

$$\frac{\Delta \vdash d \text{ meet } d' \text{ wrt } \_ \text{ ok} \quad \Delta \vdash \text{dom}(d') \sqsubseteq \text{dom}(d)}{\Delta \vdash d \text{ meet } d' \text{ wrt } \_ \text{ ok}} \text{ [MEET-GTR]}$$

$$\frac{d''' \in \{\bar{d}''\} \quad \text{name}(d) = \text{name}(d') = \text{name}(d''') \quad \Delta \vdash \text{dom}(d''') \equiv (\text{dom}(d) \cap \text{dom}(d'))}{\Delta \vdash d \text{ meet } d' \text{ wrt } \{\bar{d}''\} \text{ ok}} \text{ [MEET-THIRD]}$$

$$\frac{\text{Return Type Rule: } \Delta \vdash d \text{ return type wrt } d \text{ ok} \quad \text{Return Type Rule: } \Delta \vdash d \text{ return type wrt } d' \text{ ok} \quad \text{Return Type Rule: } \Delta \vdash d \text{ return type wrt } d' \text{ ok}}{\Delta \vdash d \text{ return type wrt } d' \text{ ok} \quad \Delta \vdash d \text{ return type wrt } d' \text{ ok} \quad \Delta \vdash d \text{ return type wrt } d' \text{ ok}} \text{ [RETURN-TRIV] [RETURN-NOT-LESS]}$$

$$\frac{\text{Return Type Rule: } \Delta \vdash d \text{ return type wrt } d \text{ ok} \quad \text{Return Type Rule: } \Delta \vdash d \text{ return type wrt } d' \text{ ok} \quad \text{Return Type Rule: } \Delta \vdash d \text{ return type wrt } d' \text{ ok}}{\Delta \vdash d \text{ return type wrt } d' \text{ ok} \quad \Delta \vdash d \text{ return type wrt } d' \text{ ok} \quad \Delta \vdash d \text{ return type wrt } d' \text{ ok}} \text{ [RETURN-TEST]}$$

Fig. 5. Overloading rules for FGFV

# Fortress: Symmetric Multiple Dispatch with Polymorphism and Variance

**PROVED**

Well-formed programs:  $\vdash \Pi : g$

$$\frac{\Pi = \bar{\psi}, e \quad \text{distinct}(\text{name}(\bar{\psi})) \quad \Delta = \{\bar{\psi}\} \quad \bar{\Delta} \vdash \bar{\psi} \text{ ok} \quad \Delta; \bullet \vdash e : (-, g)}{\vdash \Pi : g} \text{ [T-PROGRAM]}$$

Well-formed trait and object declarations:

$$\frac{\Delta' = \Delta \cup \{\{\bar{\xi}\} <: P <: \{\bar{\xi}\}\} \quad \text{disti} \quad \bar{J} = \text{properAncestors}(\Delta', T[\bar{P}]) \quad \bar{L} \quad \bar{T} \neq \text{name}(J) \quad \bar{\Delta}'; \text{self}: T[\bar{P}]; \bar{V} \bar{P}}{\Delta' \vdash d_i \text{ not duplicate of } d_j \quad \Delta' \vdash d_i \text{ return type wrt } d_j \text{ ok}} \quad \Delta \vdash \text{trait } T[\bar{V} P <$$

No Duplicates Rule:  $\Delta \vdash d$  not duplicate of  $d'$

$$\frac{\text{name}(d) \neq \text{name}(d')}{\Delta \vdash d \text{ not duplicate of } d'} \text{ [NO-DUP-TRIV]}$$

$$\frac{\neg(\Delta \vdash \text{dom}(d) \sqsubseteq \text{dom}(d'))}{\Delta \vdash d \text{ not duplicate of } d'} \text{ [NO-DUP-NOT-LESS]}$$

$$\frac{\neg(\Delta \vdash \text{dom}(d') \sqsubseteq \text{dom}(d))}{\Delta \vdash d \text{ not duplicate of } d'} \text{ [NO-DUP-NOT-GTR]}$$

Meet Rule:

$$\frac{\text{name}(d) \neq \text{name}(d') \quad \Delta \vdash d \quad \Delta \vdash d'}{\Delta \vdash (d, d')}$$

$$\frac{\Delta \vdash d \quad \Delta \vdash d'}{\Delta \vdash d}$$

Return Type Rule:  $\Delta \vdash d$  return type wrt  $d$  ok

$$\frac{\text{name}(d) \neq \text{name}(d') \quad \Delta \vdash d \text{ return type wrt } d' \text{ ok}}{\Delta \vdash d \text{ return type wrt } d' \text{ ok}} \text{ [RETURN-TRIV]}$$

$$\frac{\text{arrow}(d) = \forall[\bar{\kappa}](\alpha \rightarrow \rho) \quad \bar{\kappa} = \{\bar{\chi}\} <: P <: \{\bar{\eta}\} \quad \text{arrow}(d') = \kappa' = \{\bar{\chi}'\} <: Q <: \{\bar{\eta}'\} \quad \text{distinct}(\bar{P}, \bar{Q}) \quad \Delta \vdash \text{dom}(d) \quad \Delta \vdash \forall[\bar{\kappa}](\alpha \rightarrow \rho) \sqsubseteq \forall[\bar{\kappa}, \bar{\kappa}']((\alpha \sqcap \alpha') \rightarrow \rho')}{\Delta \vdash d \text{ return type wrt } d' \text{ ok}}$$

Well-formed method declarations:  $\Delta; \Gamma; \bar{V} \bar{P} \vdash$

$$\frac{\Delta \vdash [\{\bar{\xi}\} <: Q <: \{\bar{\xi}\}] \text{ ok} \quad \Delta' = \Delta \cup \{\{\bar{\xi}\} <: \dots\} \quad \text{distinct}(\bar{x}) \quad \bar{\Delta}' \vdash \tau \text{ ok} \quad \bar{\Delta}' \vdash \omega \text{ ok} \quad \text{distinct}(\bar{P}, \bar{Q}) \quad (\bar{V} = =) \vee (\forall \mathcal{T}. ((\bar{\tau} \rightarrow \omega) \neq \mathcal{T} [P]) \vee (\bar{\Delta} \vdash \mathcal{T} \text{ variance } V))}{\Delta; \Gamma; \bar{V} \bar{P} \vdash m[\{\bar{\xi}\} <: Q <: \{\bar{\xi}\}](\bar{x}; \bar{\tau}): \omega = e \text{ ok}} \text{ [D-METHOD]}$$

Fig. 3. Well-formed programs, class declarations, and method declarations

Well-formed ancestors:  $\Delta; \bar{J} \vdash J$  and  $J$  ancestors ok

$T \neq T'$

Existential inner subtyping:  $\Delta \vdash \Xi \lesssim \Xi$  using  $\sigma$

$$\frac{\Delta' = \Delta \cup \{\{\bar{\chi}\} <: P <: \{\bar{\eta}\}\} \quad \{\bar{P}\} \cap FV(\bar{\chi}, \bar{\eta}, \alpha') = \emptyset \quad \sigma = [\bar{\gamma}/\bar{Q}] \quad \bar{\gamma} \neq \text{Bottom}}{\Delta' \vdash \sigma \text{ on } \langle \bar{Q} \rangle \text{ obeys } \langle \bar{\chi} \rangle \text{ and } \langle \bar{\eta} \rangle} \quad \Delta' \vdash \alpha <: \sigma \alpha' \quad \Delta \vdash \exists[\{\bar{\chi}\} <: P <: \{\bar{\eta}\}] \alpha \lesssim \exists[\{\bar{\chi}'\} <: Q <: \{\bar{\eta}'\}] \alpha' \text{ using } \sigma \text{ [E-SUB]}$$

Universal inner subtyping:  $\Delta \vdash Y \lesssim Y$  using  $\sigma$

$$\frac{\Delta' = \Delta \cup \{\{\bar{\chi}'\} <: Q <: \{\bar{\eta}'\}\} \quad \{\bar{Q}\} \cap FV(\bar{\chi}, \bar{\eta}, \alpha) = \emptyset \quad \sigma = [\bar{\gamma}/\bar{P}] \quad \bar{\gamma} \neq \text{Bottom}}{\Delta' \vdash \sigma \text{ on } \langle \bar{P} \rangle \text{ obeys } \langle \bar{\chi} \rangle \text{ and } \langle \bar{\eta} \rangle} \quad \Delta' \vdash \sigma \alpha <: \alpha' \quad \Delta \vdash \forall[\{\bar{\chi}\} <: P <: \{\bar{\eta}\}] \alpha \lesssim \forall[\{\bar{\chi}'\} <: Q <: \{\bar{\eta}'\}] \alpha' \text{ using } \sigma \text{ [U-SUB]}$$

Existential reduction:  $\Delta \vdash \Xi \xrightarrow{\Xi} \Xi$  using  $\sigma$

$$\frac{\Delta \vdash \alpha \neq \text{Bottom} \Rightarrow C \quad \text{toConstraint}(\bar{K}) = C' \quad \Delta \vdash \text{unify}(C \wedge C') = (\sigma, C'') \quad \text{toBounds}(C'') = \{\bar{K}'\}}{\Delta \vdash \exists[\bar{K}] \alpha \xrightarrow{\Xi} \exists[\bar{K}'] \sigma \alpha \text{ using } \sigma} \quad \text{otherwise} \quad \Delta \vdash \exists[\bar{K}] \alpha \xrightarrow{\Xi} \exists[\bar{K}] \alpha \text{ using } []$$

Universal reduction:  $\Delta \vdash Y \xrightarrow{Y} Y$  using  $\sigma$

$$\frac{\Delta \vdash \exists[\bar{K}] \alpha \xrightarrow{\Xi} \exists[\bar{K}'] \alpha' \text{ using } \sigma}{\Delta \vdash \forall[\bar{K}] (\alpha \rightarrow \omega) \xrightarrow{\Xi} \forall[\bar{K}'] (\alpha' \rightarrow \sigma \omega) \text{ using } \sigma}$$

Existential subtyping:  $\Delta \vdash \Xi \sqsubseteq \Xi$  using  $\sigma$      $\Delta \vdash \Xi \sqsubseteq \Xi$

$$\frac{\Delta \vdash \Xi \xrightarrow{\Xi} \Xi'' \text{ using } \_ \quad \Delta \vdash \Xi'' \lesssim \Xi' \text{ using } \sigma}{\Delta \vdash \Xi \sqsubseteq \Xi' \text{ using } \sigma} \quad \frac{\Delta \vdash \Xi \sqsubseteq \Xi' \text{ using } \_}{\Delta \vdash \Xi \sqsubseteq \Xi'}$$

Universal subtyping:  $\Delta \vdash Y \sqsubseteq Y$  using  $\sigma$      $\Delta \vdash Y \sqsubseteq Y$

$$\frac{\Delta \vdash Y' \xrightarrow{\Xi} Y'' \text{ using } \_ \quad \Delta \vdash Y \lesssim Y'' \text{ using } \sigma}{\Delta \vdash Y \sqsubseteq Y' \text{ using } \sigma} \quad \frac{\Delta \vdash Y \sqsubseteq Y' \text{ using } \_}{\Delta \vdash Y \sqsubseteq Y'}$$

Fig. 6. Subtype relations of quantified types

Fig. 5. Overloading rules for FG

# Fortress: Symmetric Multiple Dispatch with Polymorphism and Variance

**PROVED**

Well-formed programs:  $\vdash \Pi : g$

$$\frac{\Pi = \bar{\psi}, e \quad \text{distinct}(\text{name}(\bar{\psi})) \quad \Delta = \{\bar{\psi}\} \quad \bar{\Delta} \vdash \bar{\psi} \text{ ok} \quad \Delta; \bullet \vdash e : (-, g)}{\vdash \Pi : g} \text{ [T-PROGRAM]}$$

Well-formed trait and object declarations:

$$\frac{\Delta' = \Delta \cup \{\{\bar{\xi}\} < P < \{\bar{\xi}\}\} \quad \text{distinct}(\bar{\xi}) \quad \{\bar{J}\} = \text{properAncestors}(\Delta', T[\bar{P}]) \quad \bar{J} \quad \bar{T} \neq \text{name}(J) \quad \bar{\Delta}'; \text{self} : T[\bar{P}]; \bar{V} \bar{P}}{\Delta' \vdash d_i \text{ not duplicate of } d_j \quad \Delta' \vdash d_i \text{ return type wrt } d_j \text{ ok} \quad \Delta \vdash \text{trait } T[\bar{V} P < \bar{\xi}]}$$

No Duplicates Rule:  $\Delta \vdash d$  not duplicate of  $d'$

$$\frac{\text{name}(d) \neq \text{name}(d')}{\Delta \vdash d \text{ not duplicate of } d'} \text{ [NO-DUP-TRIV]}$$

$$\frac{\neg(\Delta \vdash \text{dom}(d) \sqsubseteq \text{dom}(d'))}{\Delta \vdash d \text{ not duplicate of } d'} \text{ [NO-DUP-NOT-LESS]}$$

$$\frac{\neg(\Delta \vdash \text{dom}(d') \sqsubseteq \text{dom}(d))}{\Delta \vdash d \text{ not duplicate of } d'} \text{ [NO-DUP-NOT-GTR]}$$

Meet Rule:

$$\frac{\text{name}(d) \neq \text{name}(d')}{\Delta \vdash (d, d')}$$

$$\frac{\Delta \vdash d \quad \Delta \vdash d'}{\Delta \vdash (d, d')}$$

$$\frac{\Delta \vdash d \quad \Delta \vdash d'}{\Delta \vdash d}$$

Return Type Rule:  $\Delta \vdash d$  return type wrt  $d'$  ok

$$\frac{\text{name}(d) \neq \text{name}(d') \quad \neg(\Delta \vdash \text{dom}(d) \sqsubseteq \text{dom}(d'))}{\Delta \vdash d \text{ return type wrt } d' \text{ ok}} \text{ [RETURN-TRIV]}$$

$$\frac{\text{arrow}(d) = \forall[\bar{\kappa}](\alpha \rightarrow \rho) \quad \bar{\kappa} = \{\bar{\chi}\} < P < \{\bar{\eta}\} \quad \text{arrow}(d') = \forall[\bar{\kappa}'](\alpha \rightarrow \rho') \quad \bar{\kappa}' = \{\bar{\chi}'\} < Q < \{\bar{\eta}'\} \quad \text{distinct}(\bar{P}, \bar{Q}) \quad \Delta \vdash \text{dom}(d) \quad \Delta \vdash \forall[\bar{\kappa}](\alpha \rightarrow \rho) \sqsubseteq \forall[\bar{\kappa}', \bar{\kappa}']((\alpha \sqcap \alpha') \rightarrow \rho')}{\Delta \vdash d \text{ return type wrt } d' \text{ ok}}$$

Well-formed method declarations:  $\Delta; \Gamma; \bar{V} \bar{P} \vdash$

$$\frac{\Delta \vdash [\{\bar{\xi}\} < Q < \{\bar{\xi}\}] \text{ ok} \quad \Delta' = \Delta \cup \{\{\bar{\xi}\} < Q < \{\bar{\xi}\}\} \quad \text{distinct}(\bar{x}) \quad \bar{\Delta}' \vdash \tau \text{ ok} \quad \bar{\Delta}' \vdash \omega \text{ ok} \quad \text{distinct}(\bar{P}, \bar{Q}) \quad (\bar{V} = =) \vee (\forall \mathcal{T}. ((\bar{\tau} \rightarrow \omega) \neq \mathcal{T} [P]) \vee (\bar{\Delta} \vdash \mathcal{T} \text{ variance } V))}{\Delta; \Gamma; \bar{V} \bar{P} \vdash m[\{\bar{\xi}\} < Q < \{\bar{\xi}\}](\bar{x}; \bar{\tau}) : \omega = e \text{ ok}} \text{ [D-METHOD]}$$

Fig. 3. Well-formed programs, class declarations, and method declarations

Well-formed ancestors:  $\Delta; \bar{J} \vdash J$  and  $J$  ancestors ok

$T \neq T'$

Existential inner subtyping:  $\Delta \vdash \Xi \lesssim \Xi$  using  $\sigma$

$$\frac{\Delta' = \Delta \cup \{\{\bar{\chi}\} < P < \{\bar{\eta}\}\} \quad \{\bar{P}\} \cap FV(\bar{\chi}, \bar{\eta}, \alpha) = \emptyset \quad \sigma = [\bar{\gamma}/\bar{Q}] \quad \bar{\gamma} \neq \text{Bottom} \quad \Delta' \vdash \sigma \text{ on } \langle \bar{Q} \rangle \text{ obeys } \langle \bar{P} \rangle \text{ and } \langle \bar{\eta} \rangle \quad \Delta' \vdash \alpha < : \sigma \alpha'}{\Delta \vdash \exists[\{\bar{\chi}\} < P < \{\bar{\eta}\}] \alpha \lesssim \exists[\{\bar{\chi}'\} < Q < \{\bar{\eta}'\}] \alpha' \text{ using } \sigma} \text{ [E-SUB]}$$

Universal inner subtyping:  $\Delta \vdash Y \lesssim Y$  using  $\sigma$

$$\frac{\Delta' = \Delta \cup \{\{\bar{\chi}'\} < Q < \{\bar{\eta}'\}\} \quad \{\bar{Q}\} \cap FV(\bar{\chi}, \bar{\eta}, \alpha) = \emptyset \quad \sigma = [\bar{\gamma}/\bar{P}] \quad \bar{\gamma} \neq \text{Bottom} \quad \Delta' \vdash \sigma \text{ on } \langle \bar{P} \rangle \text{ obeys } \langle \bar{Q} \rangle \text{ and } \langle \bar{\eta} \rangle \quad \Delta' \vdash \sigma \alpha < : \alpha'}{\Delta \vdash \forall[\{\bar{\chi}\} < P < \{\bar{\eta}\}] \alpha \lesssim \forall[\{\bar{\chi}'\} < Q < \{\bar{\eta}'\}] \alpha' \text{ using } \sigma} \text{ [U-SUB]}$$

Many more rules ...

Universal reduction:  $\Delta \vdash Y \xrightarrow{=} Y$  using  $\sigma$

$$\frac{\Delta \vdash \exists[\bar{K}] \alpha \xrightarrow{=} \exists[\bar{K}'] \alpha' \text{ using } \sigma \quad \Delta \vdash \forall[\bar{K}] (\alpha \rightarrow \omega) \xrightarrow{=} \forall[\bar{K}'] (\alpha' \rightarrow \sigma \omega) \text{ using } \sigma}{\Delta \vdash \exists[\bar{K}] \alpha \xrightarrow{=} \exists[\bar{K}'] \alpha' \text{ using } \sigma}$$

Existential subtyping:  $\Delta \vdash \Xi \sqsubseteq \Xi$  using  $\sigma$

$$\frac{\Delta \vdash \Xi \xrightarrow{=} \Xi'' \text{ using } \sigma \quad \Delta \vdash \Xi'' \lesssim \Xi' \text{ using } \sigma}{\Delta \vdash \Xi \sqsubseteq \Xi' \text{ using } \sigma} \quad \frac{\Delta \vdash \Xi \sqsubseteq \Xi' \text{ using } \sigma}{\Delta \vdash \Xi \sqsubseteq \Xi'}$$

Universal subtyping:  $\Delta \vdash Y \sqsubseteq Y$  using  $\sigma$

$$\frac{\Delta \vdash Y' \xrightarrow{=} Y'' \text{ using } \sigma \quad \Delta \vdash Y \lesssim Y'' \text{ using } \sigma}{\Delta \vdash Y \sqsubseteq Y' \text{ using } \sigma} \quad \frac{\Delta \vdash Y \sqsubseteq Y' \text{ using } \sigma}{\Delta \vdash Y \sqsubseteq Y'}$$

Fig. 6. Subtype relations of quantified types

# Fortress: Symmetric Multiple Dispatch with Polymorphism and Variance

**PROVED**

Well-formed programs:  $\vdash \Pi : g$

$$\frac{\Pi = \bar{\psi}, e \quad \text{distinct}(\text{name}(\bar{\psi})) \quad \Delta = \{\bar{\psi}\} \quad \bar{\Delta} \vdash \bar{\psi} \text{ ok} \quad \Delta; \bullet \vdash e : (-, g)}{\vdash \Pi : g} \text{ [T-PROGRAM]}$$

Well-formed trait and object declarations:

$$\frac{\Delta' = \Delta \cup \{\{\} <: P <: \{\bar{\xi}\}\} \quad \text{disti} \quad \{\bar{J}\} = \text{properAncestors}(\Delta', T[\bar{P}]) \quad \bar{L} \quad \bar{T} \neq \text{name}(J) \quad \bar{\Delta}'; \text{self} : T[\bar{P}]; \bar{V} \bar{P}}{\Delta' \vdash d_i \text{ not duplicate of } d_j \quad \Delta' \vdash d_i \text{ return type wrt } d_j \text{ ok} \quad \Delta \vdash \text{trait } T[\bar{V} P <: \bar{L}] \text{ ok}}$$

No Duplicates Rule:  $\Delta \vdash d$  not duplicate of  $d'$

$$\frac{\text{name}(d) \neq \text{name}(d')}{\Delta \vdash d \text{ not duplicate of } d'} \text{ [NO-DUP-TRIV]}$$

$$\frac{\Delta \vdash d \text{ not duplicate of } d' \quad \neg(\Delta \vdash \text{dom}(d) \sqsubseteq \text{dom}(d'))}{\Delta \vdash d \text{ not duplicate of } d'} \text{ [NO-DUP-NOT-LESS]}$$

$$\frac{\Delta \vdash d \text{ not duplicate of } d' \quad \neg(\Delta \vdash \text{dom}(d') \sqsubseteq \text{dom}(d))}{\Delta \vdash d \text{ not duplicate of } d'} \text{ [NO-DUP-NOT-GTR]}$$

Meet Rule:

$$\frac{\Delta \vdash d \quad \Delta \vdash (d \sqcap d')}{\Delta \vdash d} \text{ [MEET]}$$

$$\frac{\Delta' = \Delta \cup \{\{\} <: P <: \{\bar{\xi}\}\} \quad \text{distin} \quad \{\bar{J}\} = \text{properAncestors}(\Delta', O[\bar{P}]) \quad \bar{\Delta}' \quad \bar{\Delta}'; \text{self} : O[\bar{P}], \bar{x} : \bar{\tau} = \bar{P} \vdash \mu \text{ ok}}{\Delta' \vdash d_i \text{ not duplicate of } d_j \quad \Delta' \vdash d_i \text{ return type wrt } d_j \text{ ok} \quad \bar{\Delta}' \vdash \tau \text{ ok} \quad \Delta \vdash \text{object } O[\bar{P} <: \{\bar{\xi}\}] \text{ ok}}$$

Return Type Rule:  $\Delta \vdash d$  return type wrt  $d$  ok

$$\frac{\text{name}(d) \neq \text{name}(d') \quad \neg(\Delta \vdash \text{dom}(d) \sqsubseteq \text{dom}(d'))}{\Delta \vdash d \text{ return type wrt } d' \text{ ok}} \text{ [RETURN-TRIV]}$$

$$\frac{\text{arrow}(d) = \forall[\bar{\kappa}](\alpha \rightarrow \rho) \quad \bar{\kappa} = \{\bar{\chi}\} <: P <: \{\bar{\eta}\} \quad \text{arrow}(d') = \forall[\bar{\kappa}'](\alpha \rightarrow \rho') \quad \bar{\kappa}' = \{\bar{\chi}'\} <: Q <: \{\bar{\eta}'\} \quad \text{distinct}(\bar{P}, \bar{Q}) \quad \Delta \vdash \text{dom}(d) \quad \Delta \vdash \forall[\bar{\kappa}](\alpha \rightarrow \rho) \sqsubseteq \forall[\bar{\kappa}', \bar{\kappa}']((\alpha \sqcap \alpha') \rightarrow \rho')}{\Delta \vdash d \text{ return type wrt } d' \text{ ok}}$$

Well-formed method declarations:  $\Delta; \Gamma; \bar{V} \bar{P} \vdash$

$$\frac{\Delta \vdash [\{\bar{\xi}\} <: Q <: \{\bar{\xi}\}] \text{ ok} \quad \Delta' = \Delta \cup \{\{\bar{\xi}\} <: Q <: \{\bar{\xi}\}\} \quad \text{distinct}(\bar{x}) \quad \bar{\Delta}' \vdash \tau \text{ ok} \quad \bar{\Delta}' \vdash \omega \text{ ok} \quad \text{distinct}(\bar{P}, \bar{Q}) \quad (\bar{V} = =) \vee (\forall \mathcal{T}. ((\bar{\tau} \rightarrow \omega) \neq \mathcal{T}[P]) \vee (\Delta \vdash \mathcal{T} \text{ variance } V))}{\Delta; \Gamma; \bar{V} \bar{P} \vdash m[\{\bar{\xi}\} <: Q <: \{\bar{\xi}\}](\bar{x} : \bar{\tau}) : \omega = e \text{ ok}} \text{ [D-METHOD]}$$

Fig. 3. Well-formed programs, class declarations, and method declarations

Well-formed ancestors:  $\Delta; \bar{J} \vdash J$  and  $J$  ancestors ok

Existential inner subtyping:  $\Delta \vdash \Xi \lesssim \Xi$  using  $\sigma$

$$\frac{\Delta' = \Delta \cup \{\{\bar{\chi}\} <: P <: \{\bar{\eta}\}\} \quad \{\bar{P}\} \cap \text{FV}(\bar{\chi}, \bar{\eta}, \alpha') = \emptyset \quad \sigma = [\bar{\gamma}/\bar{Q}] \quad \bar{\gamma} \neq \text{Bottom} \quad \Delta' \vdash \sigma \text{ on } \langle \bar{Q} \rangle \text{ obeys } \langle \bar{P} \rangle \text{ and } \langle \bar{\eta}' \rangle \quad \Delta' \vdash \alpha <: \sigma \alpha'}{\Delta \vdash \exists[\{\bar{\chi}\} <: P <: \{\bar{\eta}\}] \alpha \lesssim \exists[\{\bar{\chi}'\} <: Q <: \{\bar{\eta}'\}] \alpha' \text{ using } \sigma} \text{ [E-SUB]}$$

Universal inner subtyping:  $\Delta \vdash Y \lesssim Y$  using  $\sigma$

$$\frac{\Delta' = \Delta \cup \{\{\bar{\chi}'\} <: Q <: \{\bar{\eta}'\}\} \quad \{\bar{Q}\} \cap \text{FV}(\bar{\chi}, \bar{\eta}, \alpha) = \emptyset \quad \sigma = [\bar{\gamma}/\bar{P}] \quad \bar{\gamma} \neq \text{Bottom} \quad \Delta' \vdash \sigma \text{ on } \langle \bar{P} \rangle \text{ obeys } \langle \bar{Q} \rangle \text{ and } \langle \bar{\eta} \rangle \quad \Delta' \vdash \sigma \alpha <: \alpha'}{\Delta \vdash \forall[\{\bar{\chi}\} <: P <: \{\bar{\eta}\}] \alpha \lesssim \forall[\{\bar{\chi}'\} <: Q <: \{\bar{\eta}'\}] \alpha' \text{ using } \sigma} \text{ [U-SUB]}$$

Next: Coq Mechanization

Universal reduction:  $\Delta \vdash Y \xrightarrow{=} Y$  using  $\sigma$

$$\frac{\Delta \vdash \exists[\bar{K}'] \alpha \xrightarrow{=} \exists[\bar{K}'] \alpha' \text{ using } \sigma \quad \Delta \vdash \forall[\bar{K}] (\alpha \rightarrow \omega) \xrightarrow{=} \forall[\bar{K}'] (\alpha' \rightarrow \sigma \omega) \text{ using } \sigma}{\Delta \vdash \exists[\bar{K}] \alpha \xrightarrow{=} \exists[\bar{K}'] \alpha' \text{ using } \sigma} \text{ [UNIV-RED]}$$

Existential subtyping:  $\Delta \vdash \Xi \sqsubseteq \Xi$  using  $\sigma$

$$\frac{\Delta \vdash \Xi \xrightarrow{=} \Xi'' \text{ using } \sigma \quad \Delta \vdash \Xi'' \lesssim \Xi' \text{ using } \sigma}{\Delta \vdash \Xi \sqsubseteq \Xi' \text{ using } \sigma} \text{ [EXIST-SUB]}$$

Universal subtyping:  $\Delta \vdash Y \sqsubseteq Y$  using  $\sigma$

$$\frac{\Delta \vdash Y' \xrightarrow{=} Y'' \text{ using } \sigma \quad \Delta \vdash Y \lesssim Y'' \text{ using } \sigma}{\Delta \vdash Y \sqsubseteq Y' \text{ using } \sigma} \text{ [UNIV-SUB]}$$

Fig. 6. Subtype relations of quantified types

# Fortress: Symmetric Multiple Dispatch with Polymorphism and Variance

**PROVED**

<p><b>No Duplicates Rule:</b> <math>\Delta \vdash d</math> not duplicate of <math>d</math></p> $\frac{\text{name}(d) \neq \text{name}(d')}{\Delta \vdash d \text{ not duplicate of } d'} \quad [\text{NO-DUP-TRIV}]$ $\frac{\neg(\Delta \vdash \text{dom}(d) \sqsubseteq \text{dom}(d'))}{\Delta \vdash d \text{ not duplicate of } d'} \quad [\text{NO-DUP-NOT-LESS}]$ $\frac{\neg(\Delta \vdash \text{dom}(d') \sqsubseteq \text{dom}(d))}{\Delta \vdash d \text{ not duplicate of } d'} \quad [\text{NO-DUP-NOT-GTR}]$	<p><b>Meet Rule:</b> <math>\Delta \vdash d</math> meet <math>d</math> wrt <math>\{\bar{d}\}</math> ok</p> $\frac{\text{name}(d) \neq \text{name}(d')}{\Delta \vdash d \text{ meet } d' \text{ wrt } \_ \text{ ok}} \quad [\text{MEET-TRIV}]$ $\frac{\Delta \vdash (\text{dom}(d) \sqcap \text{dom}(d')) \sqsubseteq \exists \llbracket \_ \rrbracket \text{Bottom}}{\Delta \vdash d \text{ meet } d' \text{ wrt } \_ \text{ ok}} \quad [\text{MEET-EXCL}]$ $\frac{\Delta \vdash \text{dom}(d) \sqsubseteq \text{dom}(d')}{\Delta \vdash d \text{ meet } d' \text{ wrt } \_ \text{ ok}} \quad [\text{MEET-LESS}]$ $\frac{\Delta \vdash \text{dom}(d') \sqsubseteq \text{dom}(d)}{\Delta \vdash d \text{ meet } d' \text{ wrt } \_ \text{ ok}} \quad [\text{MEET-GTR}]$ $\frac{d''' \in \{\bar{d}''\} \quad \text{name}(d) = \text{name}(d') = \text{name}(d''') \quad \Delta \vdash \text{dom}(d''') \equiv (\text{dom}(d) \sqcap \text{dom}(d'))}{\Delta \vdash d \text{ meet } d' \text{ wrt } \{\bar{d}''\} \text{ ok}} \quad [\text{MEET-THIRD}]$
<p><b>Return Type Rule:</b> <math>\Delta \vdash d</math> return type wrt <math>d</math> ok</p> $\frac{\text{name}(d) \neq \text{name}(d')}{\Delta \vdash d \text{ return type wrt } d' \text{ ok}} \quad [\text{RETURN-TRIV}]$ $\frac{\text{arrow}(d) = \forall \llbracket \bar{\kappa} \rrbracket (\alpha \rightarrow \rho) \quad \bar{\kappa} = \{\bar{\chi}\} <: P <: \{\bar{\eta}\}}{\Delta \vdash \forall \llbracket \bar{\kappa} \rrbracket (\alpha \rightarrow \rho) \sqsubseteq \forall \llbracket \bar{\kappa}, \bar{\kappa}' \rrbracket ((\alpha \sqcap \alpha') \rightarrow \rho')}} \quad [\text{RETURN-TEST}]$	$\frac{\neg(\Delta \vdash \text{dom}(d) \sqsubseteq \text{dom}(d'))}{\Delta \vdash d \text{ return type wrt } d' \text{ ok}} \quad [\text{RETURN-NOT-LESS}]$ $\frac{\text{arrow}(d') = \forall \llbracket \bar{\kappa}' \rrbracket (\alpha' \rightarrow \rho') \quad \bar{\kappa}' = \{\bar{\chi}'\} <: Q <: \{\bar{\eta}'\} \quad \text{distinct}(\bar{P}, \bar{Q}) \quad \Delta \vdash \text{dom}(d) \sqsubseteq \text{dom}(d')}{\Delta \vdash d \text{ return type wrt } d' \text{ ok}} \quad [\text{RETURN-TEST}]$

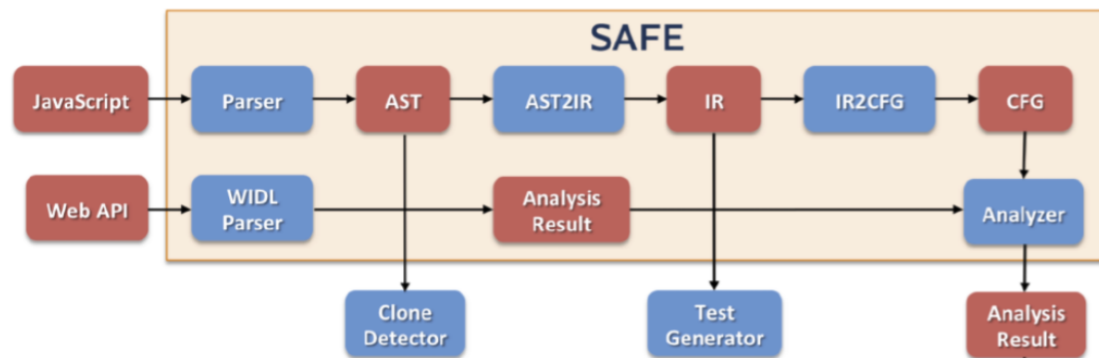
Fig. 5. Overloading rules for FGFV

# Language *Manipulation*: JavaScript

- Specification: ECMAScript
- Parsing: automatic generation of parsers & ASTs
- Static checking: parallel development
- Compilation / Interpretation: cross validation
- Testing
- Analysis: SAFE, TAJIS, WALA
- Verification



# Analyzing JS



```

module M {s...}
module M = M...M;
import M...x;
import M...x: x;
import M...*;
export var x [= e];
export function x(x...) {s...}
export module M {s...}
export module M = M...M;
export x;
export x: x;
export x: M...x;
  
```

Figure 9. Extended syntax for JavaScript modules

```

v ::= ... | α      value
α ::= ⟨⟨vg⟩⟩     accessor
vg ::= func(){ return e }  getter
  
```

Figure 10. Extended syntax for λ<sub>JS</sub> to allow accessors

```

module definition
module alias
qualified import
aliased import
import all
exported variable
exported function
exported module
exported module alias
exported local
exported local alias
exported qualified alias
  
```

```

φ ::= x...
φi ::= φ.(x)
φe ::= φ.x
φ ::= φi
      | φe
φ̄ ::= φ.*
τ ::= var
      | module
ς ::= ε
      | local
      | export φe
ρ ::= ⊥
      | τ φ
ρ̄ ::= ⊥
      | τ
Σ ::= {(φ, ρς) ...}
      ∪ {(φ̄, ρ̄) ...}
Σ* ::= ε
      | Σ* Σ
      | Σ* x
  
```

Figure 12. Desugaring environment for the modified λ<sub>JS</sub>

Hongki Lee, Sooncheol Won, Joonho Jin, Junhee Cho, and Sukyoung Ryu. **SAFE: Formal Specification and Implementation of a Scalable Analysis Framework for ECMAScript** (FOOL'12)

Seonghoon Kang and Sukyoung Ryu. **Formal Specification of a JavaScript Module System** (OOPSLA'12)

Changhee Park, Hongki Lee, and Sukyoung Ryu. **All about the “with” Statement in JavaScript: Removing “with” Statements in JavaScript Applications** (DLS'13)

WaiTing Cheung, Sukyoung Ryu, Sunghun Kim. **Development Nature Matters: An Empirical Study of Code Clones in JavaScript Applications** (EMSE'15)

# Analyzing JS

```

module M {s...}
module M = M...M;
import M...x;
    
```

```

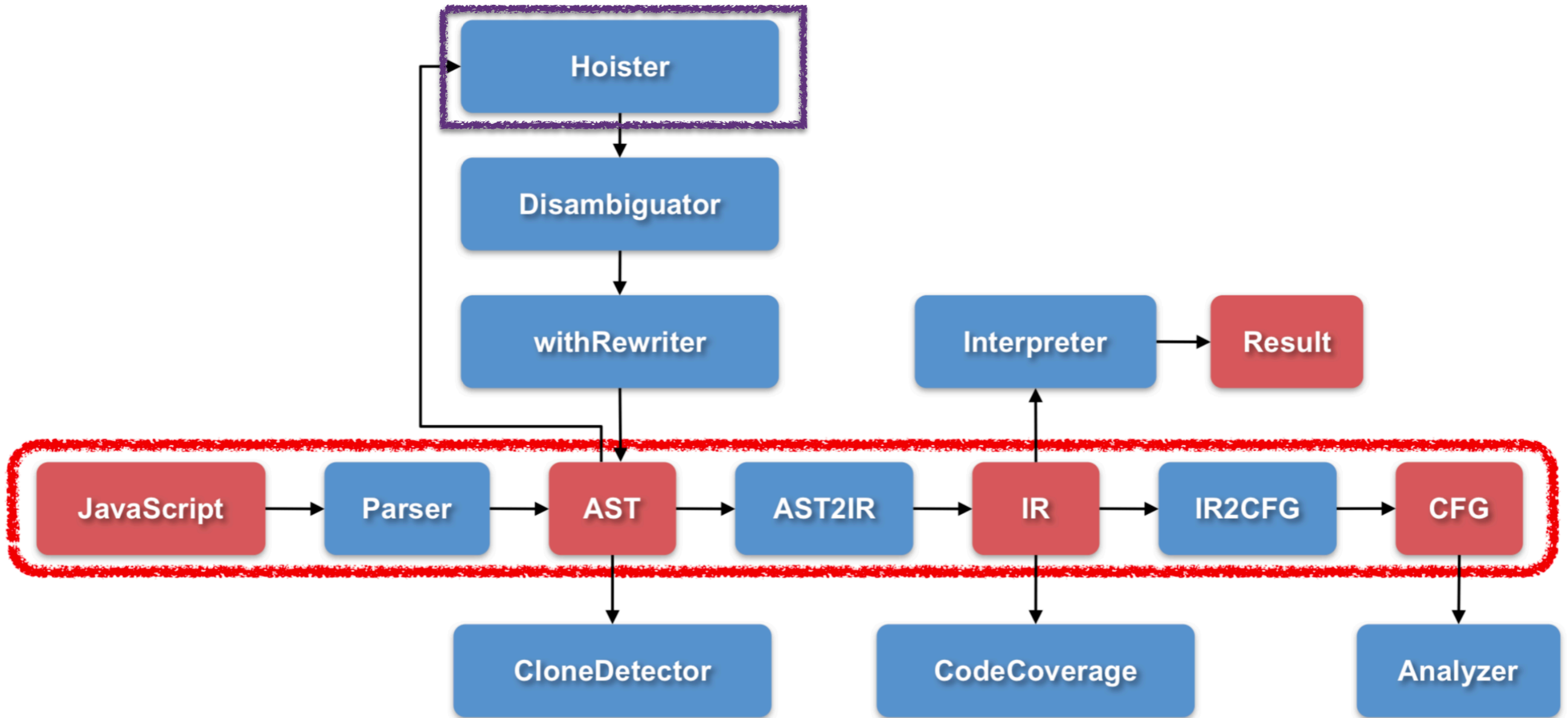
module definition
module alias
qualified import
    
```

```

 $\phi ::= x \dots$ 
 $\varphi_i ::= \phi.(x)$ 
 $\varphi_e ::= \phi.x$ 
    
```

```

path
internal qualified name
external qualified name
    
```

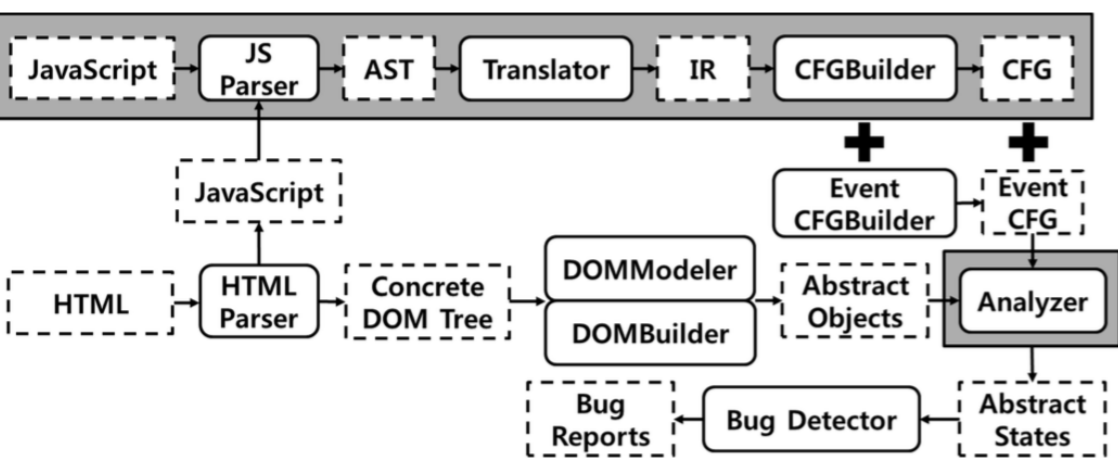
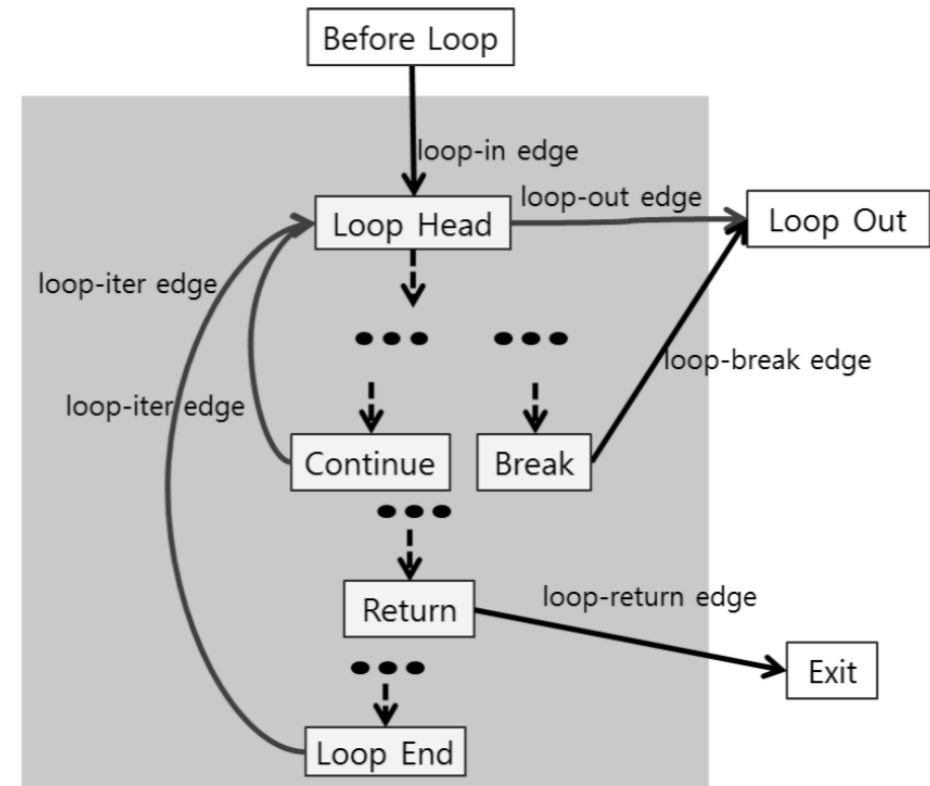
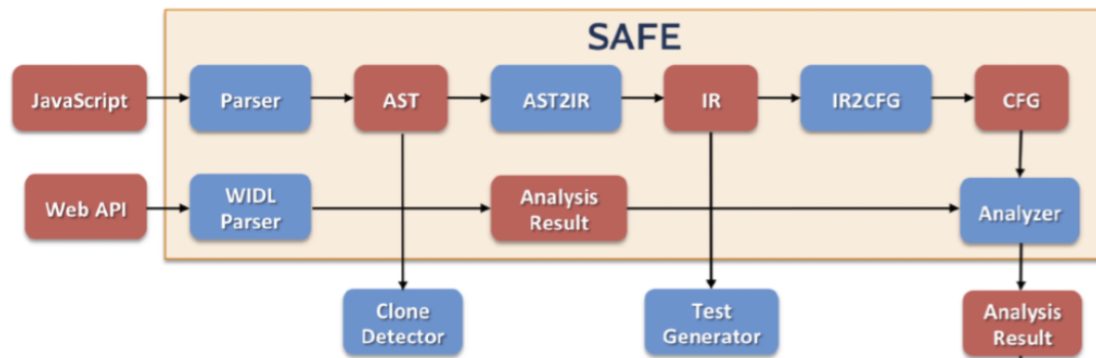


Changhee Park, Hongki Lee, and Sukyoung Ryu. **All about the “with” Statement in JavaScript: Removing “with” Statements in JavaScript Applications** (DLS’13)

WaiTing Cheung, Sukyoung Ryu, **Sunghun Kim**. **Development Nature Matters: An Empirical Study of Code Clones in JavaScript Applications** (EMSE’15)



# Analyzing JS Web Apps

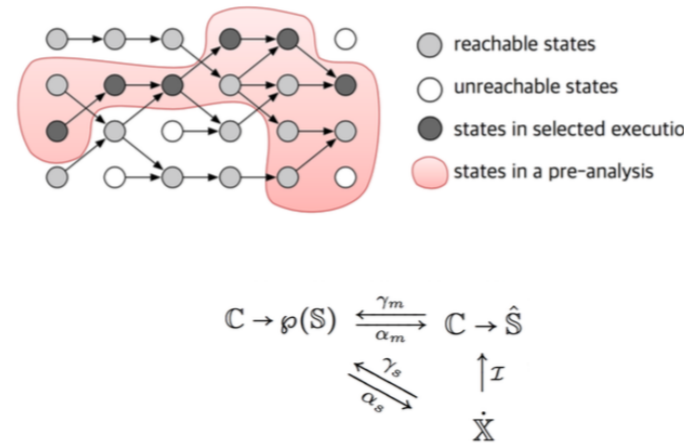
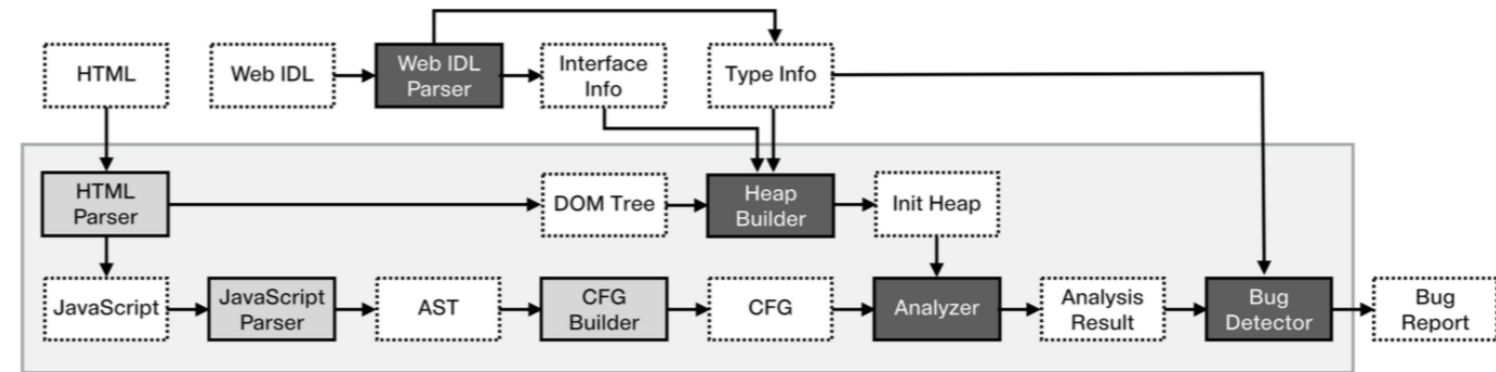
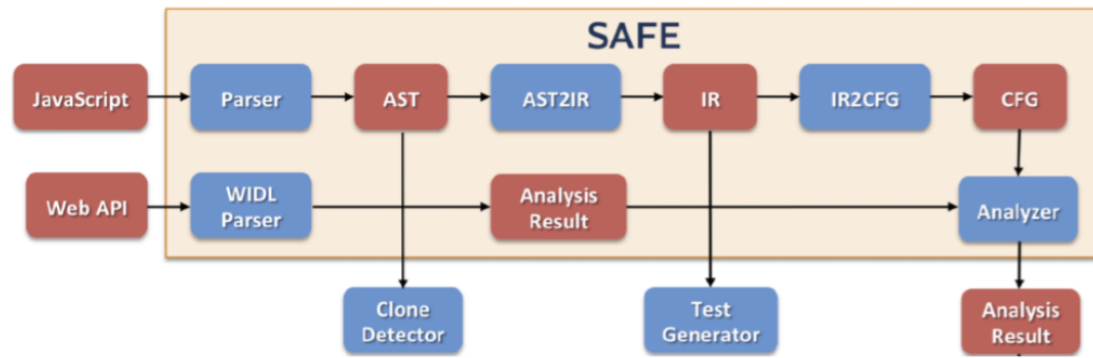


Changhee Park, Sooncheol Won, Joonho Jin, and Sukyoung Ryu. **Static Analysis of JavaScript Web Applications in the Wild via Practical DOM Modeling** (ASE'15)



Changhee Park and Sukyoung Ryu. **Scalable and Precise Static Analysis of JavaScript Applications via Loop-Sensitivity** (ECOOP'15)

# Analyzing JS Web Apps in the Wild

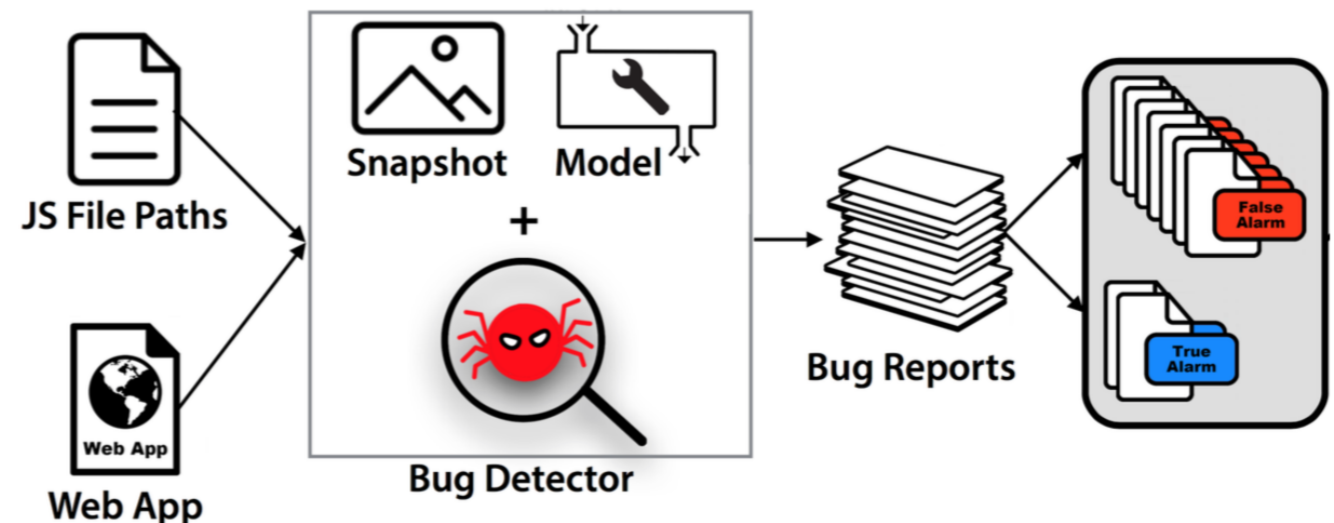
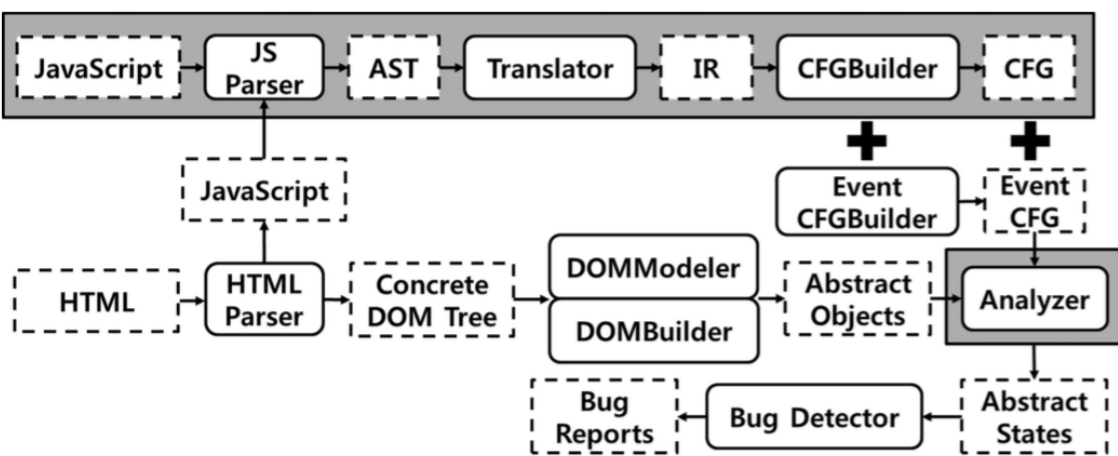
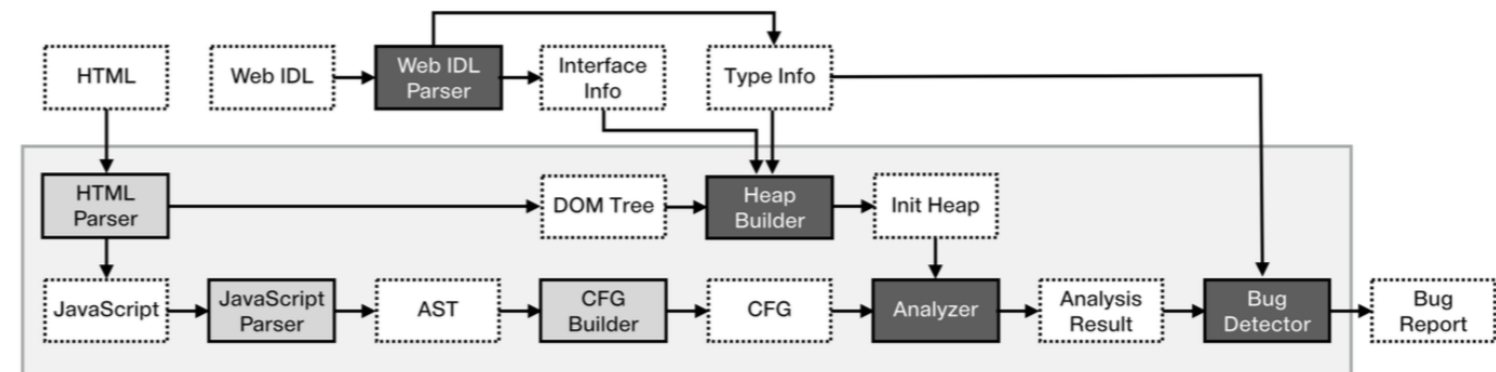
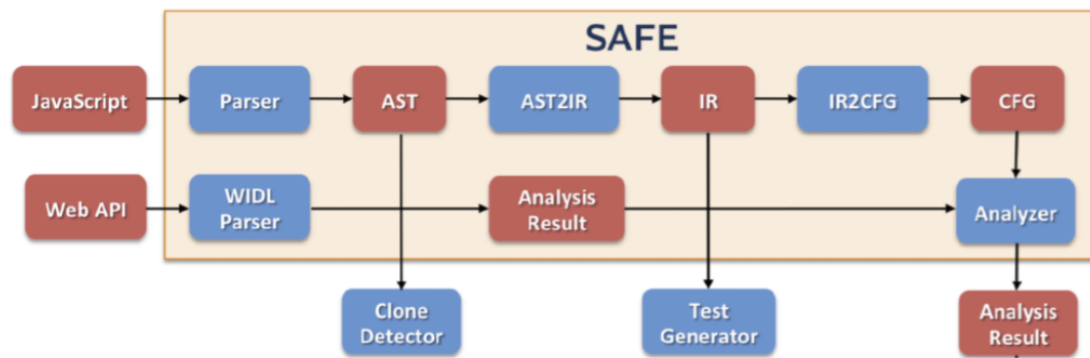


	Subject (LOC)	SAFE	SWP	SWF
Benchmark	RayTrace (679)	×	576.3 (4.8/571.5)	600.3 (2.9/597.4)
	Richards (288)	2.1	3.7 (2.4/1.3)	3.9 (2.2/1.7)
	Splay (205)	9.2	8.6 (2.1/6.5)	15.8 (1.8/14.0)
	NavierStokes (331)	1.0	4.4 (3.1/1.3)	3.2 (2.0/1.2)
	Box2dWeb (10918)	45.0	58.5 (15.6/42.9)	48.2 (45.4/2.8)
Library	jQuery (6206)	×	×	28.6 (23.9/4.7)
	MooTools (4022)	×	×	27.6 (25.7/1.9)
	Prototype (5914)	×	×	26.2 (24.2/2.0)
	YUI (7181)	×	8.6 (6.9/1.7)	18.7 (13.7/5.0)
	Underscore (1065)	×	×	5.2 (4.6/0.6)
Website	live.com (6325)	240.8	×	128.0 (32.2/95.8)
	wikipedia.org (291)	0.1	5.8 (5.8/0.0)	5.8 (5.8/0.0)
	facebook.com (5584)	×	×	64.1 (62.1/2.0)
	youtube.com (5061)	×	×	382.6 (247.6/135.0)
	baidu.com (9739)	×	×	119.0 (100.2/18.8)

SungGyeong Bae, **Hyunghun Cho**, Inho Lim, and Sukyoung Ryu. **SAFE<sub>WAPI</sub>: Web API Misuse Detector for Web Applications** (FSE'14)

Yoonseok Ko, Hongki Lee, **Julian Dolby**, and Sukyoung Ryu. **Practically Tunable Static Analysis Framework for Large-Scale JavaScript Applications** (ASE'15)

# Analyzing JS Web Apps in the Wild Partially



Joonyoung Park, **Inho Lim**, and Sukyoung Ryu. **Battles with False Positives in Static Analysis of JavaScript Web Applications in the Wild** (ICSE-SEIP'16)

Joonyoung Park, **Kwangwon Sun**, and Sukyoung Ryu. **EventHandler-based Analysis Framework for Web Apps using Dynamically Collected States** (FASE'18)

# Analyzing JS Web Apps in the Wild Partially

## JavaScript Bug Detection

```

3d-raytrace.js:118:19~118:23: [Warning] Trying to convert undefined to number. 'self[3]' can be undefined.
3d-raytrace.js:118:19~118:23: [Warning] Reading absent property '3' of object 'self'.
3d-raytrace.js:119:19~119:23: [Warning] Trying to convert undefined to number. 'self[7]' can be undefined.
3d-raytrace.js:119:19~119:23: [Warning] Reading absent property '7' of object 'self'.
3d-raytrace.js:120:19~120:24: [Warning] Trying to convert undefined to number. 'self[11]' can be undefined.
3d-raytrace.js:120:19~120:24: // this camera code is from notes i made ages ago, it is from
                             *somewhere* -- i cannot remember where
                             // that somewhere is
function invertMatrix(self) {
  var temp = new Array(11);
  var tx = -self[3];
  var ty = -self[7];
  var tz = -self[11];
  for (h = 0; h < 3; h++)
    for (v = 0; v < 3; v++)
      temp[h + v * 4] = self[h + v * 4];
  for (i = 0; i < 11; i++)
    self[i] = temp[i];
  self[3] = tx * self[0] + ty * self[4] + tz * self[8];
  self[7] = tx * self[1] + ty * self[5] + tz * self[9];
  self[11] = tx * self[2] + ty * self[6] + tz * self[10];
}

function Camera(origin, lookat, up) {
  var zaxis = normaliseVector(subVector(lookat, origin));
  var xaxis = normaliseVector(cross(up, zaxis));
  var yaxis = normaliseVector(cross(xaxis, subVector([0,0,0], zaxis)));
  var m = new Array(16);
  m[0] = xaxis[0]; m[1] = xaxis[1]; m[2] = xaxis[2];
  m[4] = yaxis[0]; m[5] = yaxis[1]; m[6] = yaxis[2];
  m[8] = zaxis[0]; m[9] = zaxis[1]; m[10] = zaxis[2];
  invertMatrix(m);
  m[3] = 0; m[7] = 0; m[11] = 0;
  this.origin = origin;
}
    
```

## Web Page Bug Detection (I)



## Web Application Bug Detection (I)



```

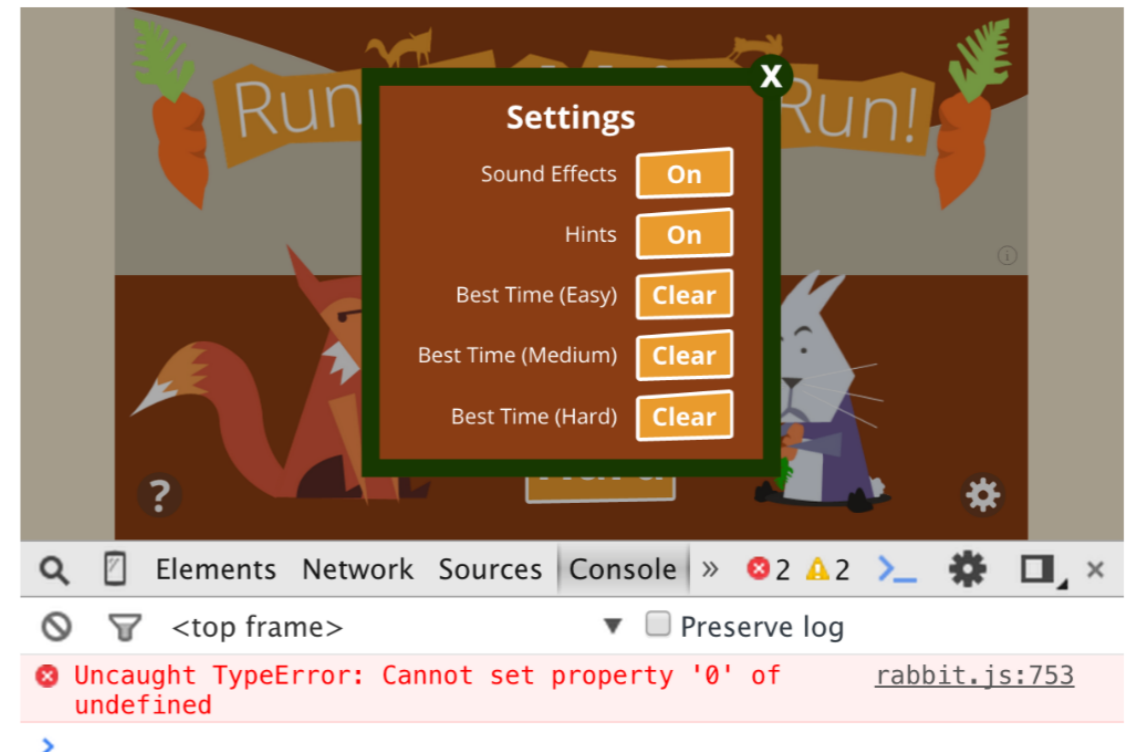
loading : function(i) {
  // alert("<img src='image/loading_" + i + ".png'>");
  var tmpdivB = document.getElementById("waitIcon");

  i = i == null ? 1 : i;

  // set timeout is 30s
  this.totalCnt++;
  if (this.totalCnt > 200) {
    this.endLoading();
    tmpdivB.className = "";
    this.showNoResultFound(tmpdivB);
    return;
  }
}
    
```

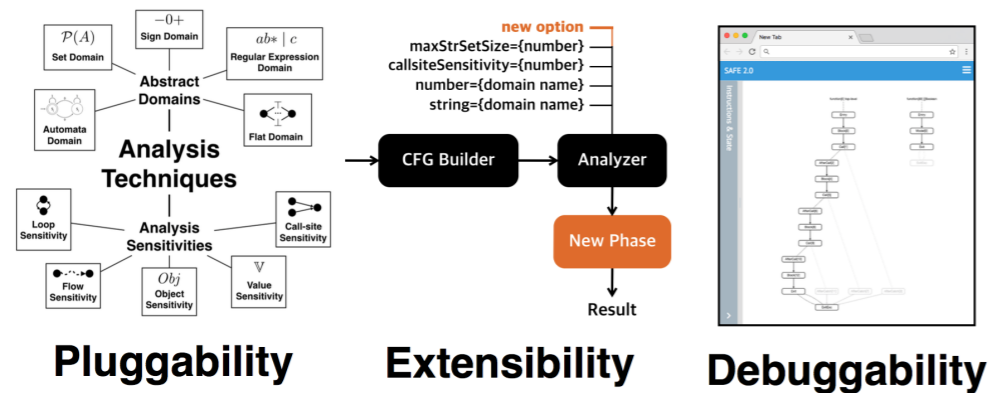
```

<div id="waitIconDiv" class="waitIconType" style="display:none;">
  <img src = "css/images/009.gif" width = "50px" height = "50px"/>
</div>
    
```



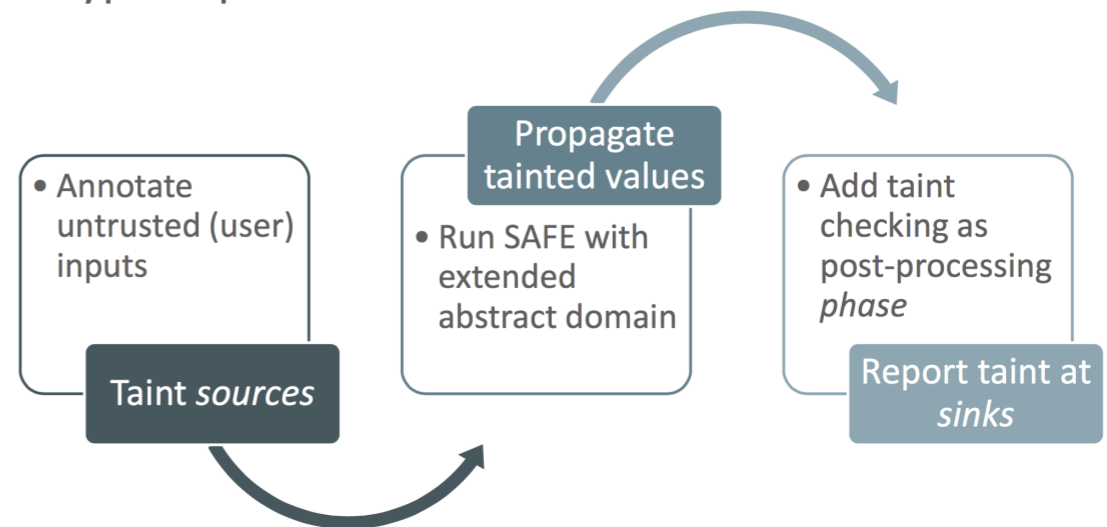
# Bug Detection in JS Web Apps with SAFE

## SAFE 2.0

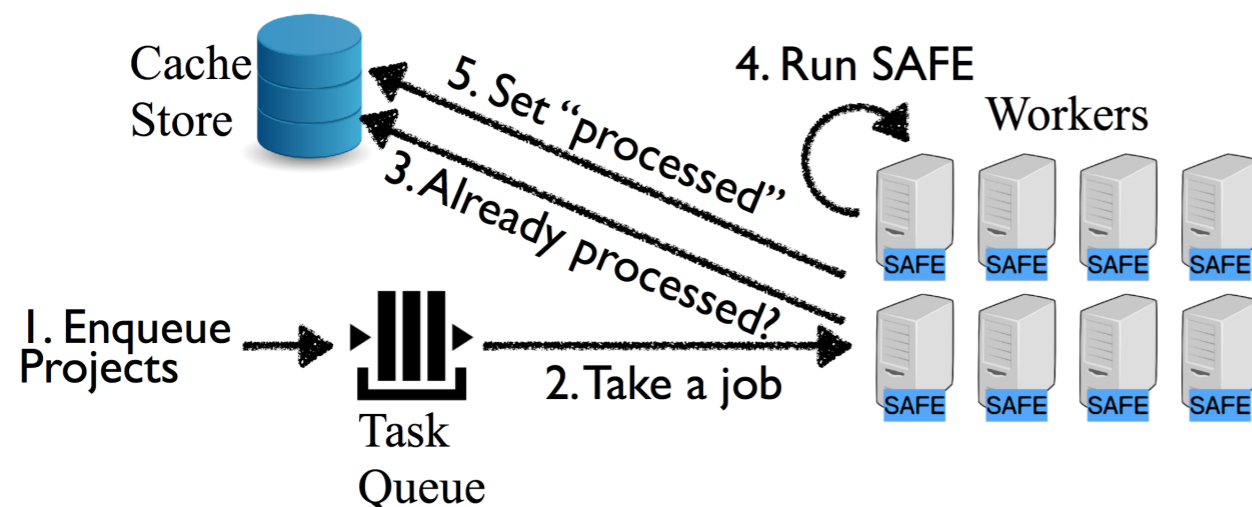


<https://github.com/sukyoung/safe>

## Prototype Implementation in SAFE



## Procedure



## Revisiting Recency Abstraction for JavaScript

Towards an Intuitive, Compositional, and Efficient Heap Abstraction  
**Singleton Abstraction**

Jihyeok Park

KAIST

Xavier Rival

DIENS, ÉNS, CNRS,  
PSL Research University  
and INRIA

Sukyoung Ryu

KAIST

# Now, Solidity!



**coindesk**  
**The DAO Attacked: Code Issue Leads to \$60 Million Ether Theft**



 Michael del Castillo     
 Jun 17, 2016 at 14:00 UTC | Updated Jun 18, 2016 at 14:46 UTC

NEWS

The DAO, the distributed autonomous organization that had collected over \$150m worth of the cryptocurrency ether, has reportedly been hacked, sparking a broad market sell-off.

A leaderless organization comprised of a series of smart contracts written on the ethereum codebase, The DAO has lost 3.6m ether, which is currently sitting in a separate wallet after being split off into a separate grouping dubbed a "child DAO"

<http://www.dailymail.co.uk/sciencetech/article-5062543/200-MILLION-virtual-currency-Ether-lost.html>

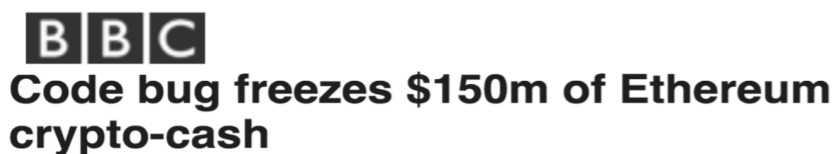
<https://www.coindesk.com/dao-attacked-code-issue-leads-60-million-ether-theft/>



**MailOnline** | TV&Showbiz | Femail | Health | **Science** | Money | Video  
 Discounts

## £200 million worth of digital cryptocurrency is wiped out as bungling developer locks investors out while trying to stop hackers

- A developer was fixing a bug that let hackers steal funds from virtual wallets
- But the developer accidentally left a second flaw in its systems
- When the user tried to undo the damage by deleting the flaw in the code, this locked the funds in the wallets permanently
- The only way to reverse the issue is a 'hard-fork', but not everyone supports this



**BBC**  
**Code bug freezes \$150m of Ethereum crypto-cash**

9 November 2017



<http://www.bbc.com/news/technology-41928147>



## Hackers Have Walked Off With About 14% of Big Digital Currencies

By **Olga Kharif**  
 January 18, 2018, 7:19 PM GMT+5:30

- Cybercriminals compromise Bitcoin, Ether supply, blockchains
- Crypto-crazed users adopt technology without weighing risks

<https://www.bloomberg.com/news/articles/2018-01-18/hackers-have-walked-off-with-about-14-of-big-digital-currencies>

# Smart Contract Vulnerabilities

## Schneier on Security

[Blog](#)[Newsletter](#)[Books](#)[Essays](#)[News](#)[Talks](#)[Academic](#)[About Me](#)[Blog](#) >

### Ethereum Hacks

The [press is reporting](#) a \$32M theft of the cryptocurrency Ethereum. Like all such thefts, they're not a result of a cryptographic failure in the currencies, but instead a software vulnerability in the software surrounding the currency -- in this case, digital wallets.

This is the second Ethereum hack this week. [The first](#) tricked people in sending their Ethereum to another address.

This is my concern about digital cash. The cryptography can be bulletproof, but the computer security will always be an issue.

Tags: [cryptocurrency](#), [cryptography](#), [hacking](#), [theft](#), [vulnerabilities](#)

Posted on July 20, 2017 at 9:12 AM • 46 Comments

#### About Bruce Schneier



I've been writing about security issues on my [blog](#) since 2004, and in my monthly [newsletter](#) since 1998. I write [books](#), [articles](#), and [academic papers](#). Currently, I'm the Chief Technology Officer of [IBM Resilient](#), a fellow at Harvard's [Berkman Center](#), and a board member of [EFF](#).

# Smart Contract Vulnerabilities: Research

ETHEREUM: A SECURE DECENTRALISED GENERALISED TRANSACTION LEDGER BYZANTIUM VERSION d1ca9d0 - 2018-03-0827

## 0s: Stop and Arithmetic Operations

All arithmetic is modulo  $2^{256}$  unless otherwise noted. The zero-th power of zero  $0^0$  is defined to be one.

Value	Mnemonic	$\delta$	$\alpha$	Description
0x00	STOP	0	0	Halts execution.
0x01	ADD	2	1	Addition operation. $\mu'_s[0] \equiv \mu_s[0] + \mu_s[1]$
0x02	MUL	2	1	Multiplication operation. $\mu'_s[0] \equiv \mu_s[0] \times \mu_s[1]$
0x03	SUB	2	1	Subtraction operation. $\mu'_s[0] \equiv \mu_s[0] - \mu_s[1]$
0x04	DIV	2	1	Integer division operation. $\mu'_s[0] \equiv \begin{cases} 0 & \text{if } \mu_s[1] = 0 \\ \lfloor \mu_s[0] \div \mu_s[1] \rfloor & \text{otherwise} \end{cases}$
0x05	SDIV	2	1	Signed integer division operation (truncated). $\mu'_s[0] \equiv \begin{cases} 0 & \text{if } \mu_s[1] = 0 \\ -2^{255} & \text{if } \mu_s[0] = -2^{255} \wedge \mu_s[1] = -1 \\ \text{sgn}(\mu_s[0] \div \mu_s[1]) \lfloor  \mu_s[0] \div \mu_s[1]  \rfloor & \text{otherwise} \end{cases}$

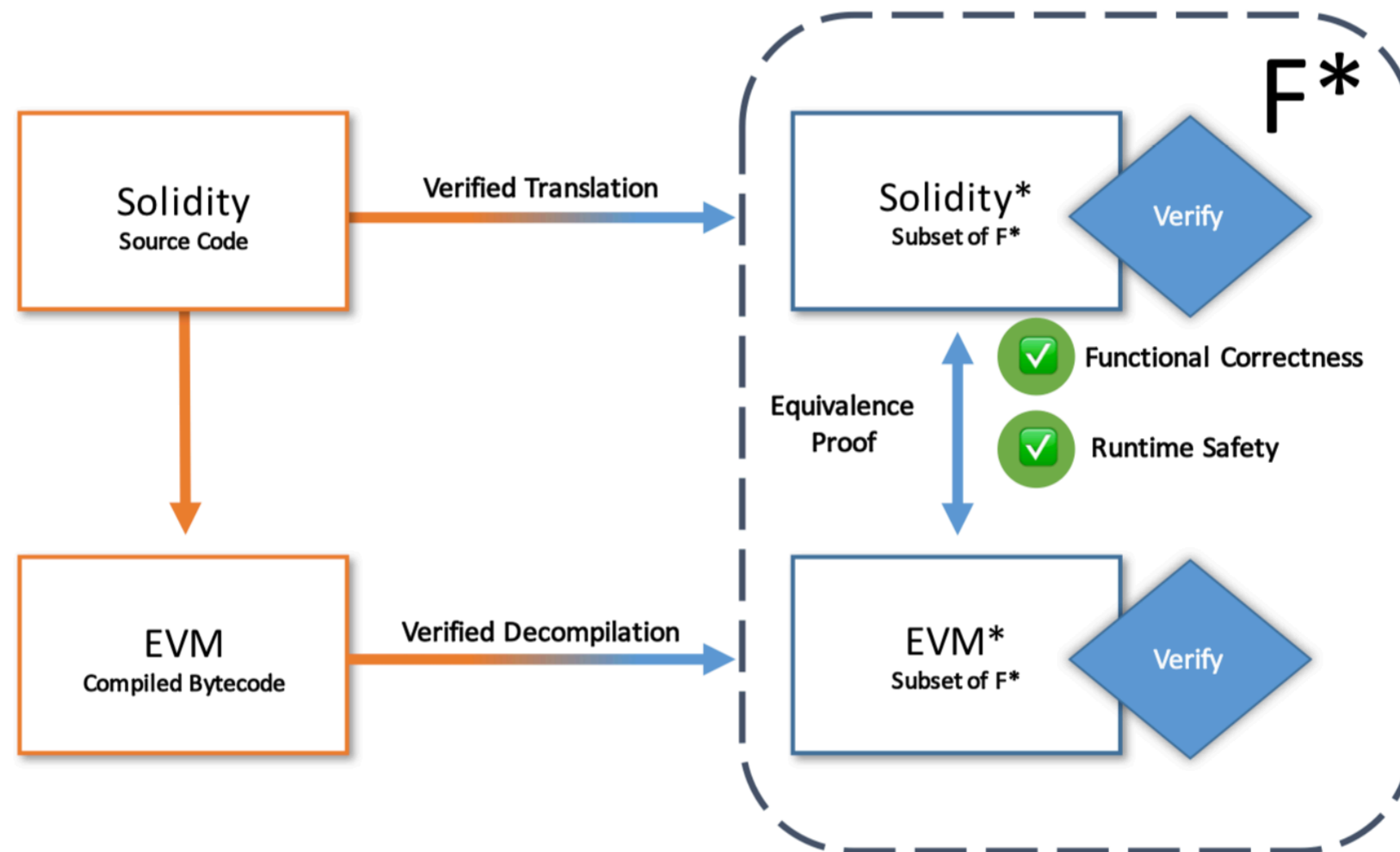
Where all values are treated as two's complement signed 256-bit integers. Note the overflow semantic when  $-2^{255}$  is negated.

<https://ethereum.github.io/yellowpaper/paper.pdf>



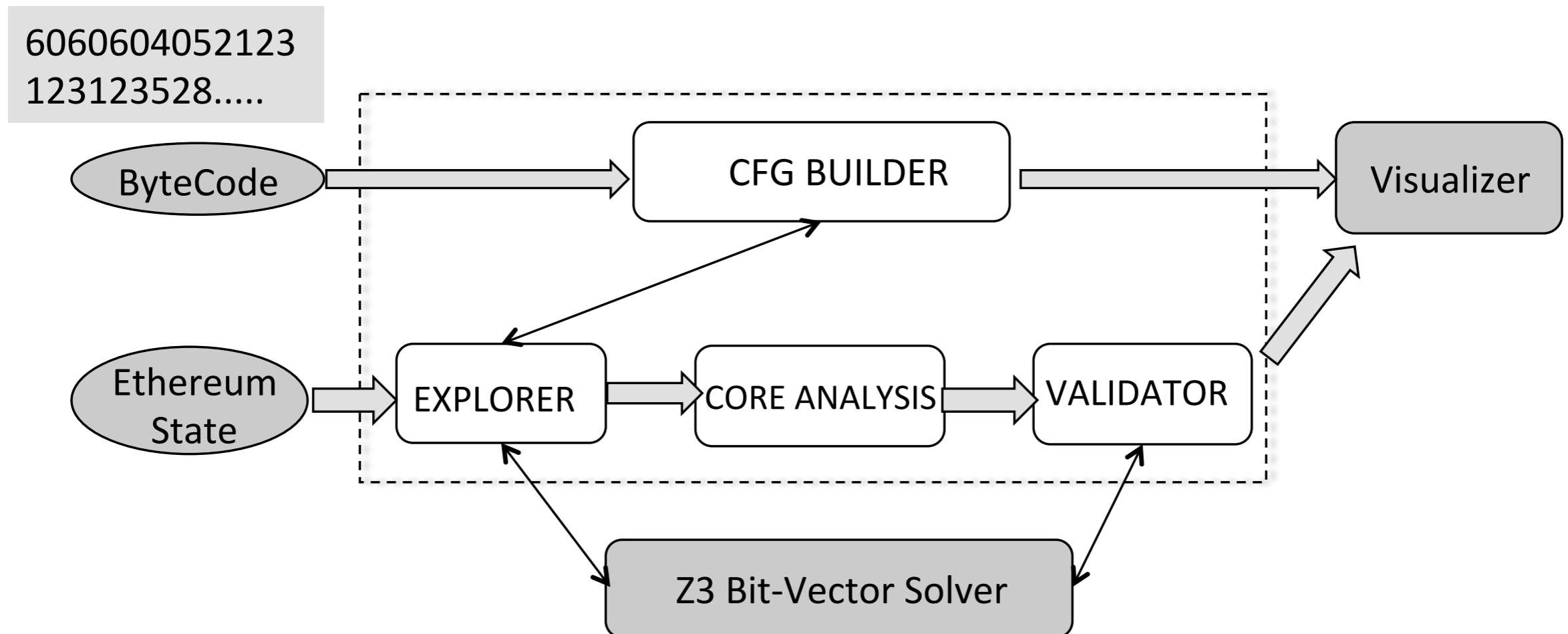
# Smart Contract Vulnerabilities: Research

- Formal Verification of Smart Contracts, PLAS 2016
  - ◆ A small subset of the Solidity programming language
  - ◆ A tiny language and no automatic verification



# Smart Contract Vulnerabilities: Research

- Making Smart Contracts Smarter, CCS 2016
  - ◆ Oyente: Symbolic execution of EVM bytecode
  - ◆ Not sound nor complete



# Smart Contract Vulnerabilities: Research

- A Survey of Attacks on Ethereum Smart Contracts, POST 2017

Level	Cause of vulnerability	Attacks
Solidity	Call to the unknown	4.1
	Gasless send	4.2
	Exception disorders	4.2, 4.5
	Type casts	—
	Reentrancy	4.1
	Keeping secrets	4.3
EVM	Immutable bugs	4.4, 4.5
	Ether lost in transfer	—
	Stack size limit	4.5
Blockchain	Unpredictable state	4.5, 4.6
	Generating randomness	—
	Time constraints	4.5

**Table 1.** Taxonomy of vulnerabilities in Ethereum smart contracts.

# Smart Contract Vulnerabilities: Research

- Zeus: Analyzing Safety of Smart Contracts, NDSS 2018
  - ◆ Verification using an LLVM model checker after compiling Solidity code to LLVM bitcode



# Smart Contract Vulnerabilities: Research

- A Semantic Framework for the Security Analysis of Ethereum Smart Contracts, POST 2018

## Formal guarantees

- ▶ We prove our abstraction to be sound:
  - “Every concrete execution can be mimicked by derivations in the abstract semantics”

$$\begin{array}{c}
 \text{artificial id of contract } c \\
 \text{(in accordance with } C_{\text{call}}) \quad \Gamma \models s_c :: S \xrightarrow{*} S' + + S \quad \text{set of known contracts} \\
 \Rightarrow \underbrace{\beta_s(s, id, 0)}_{\substack{\text{encoding of execution} \\ \text{state} \\ \text{as predicate instances}}} \cup \underbrace{\beta_c(C_{\text{call}}, id)}_{\substack{\text{encoding of program} \\ \text{logics of known contracts} \\ \text{as horn clauses}}} \vdash \underbrace{\beta_S(S', C_{\text{call}}, id, 0)}_{\substack{\text{encoding of call stack} \\ \text{as predicate instances}}}
 \end{array}$$

# Smart Contract Vulnerabilities: Research

## ■ USENIX Security 2018

### Track 1

#### Smart Contracts

[Hide details](#) ▼

Session Chair: Suman Jana, *Columbia University*

#### [teEther: Gnawing at Ethereum to Automatically Exploit Smart Contracts](#)

Johannes Krupp and Christian Rossow, *CISPA, Saarland University, Saarland Informatics Campus*

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#### [Enter the Hydra: Towards Principled Bug Bounties and Exploit-Resistant Smart Contracts](#)

Lorenz Breidenbach, *Cornell Tech, IC3, ETH Zurich*; Philip Daian, *Cornell Tech, IC3*; Florian Tramer, *Stanford*; Ari Juels, *Cornell Tech, IC3, Jacobs Institute*

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#### [Arbitrum: Scalable, private smart contracts](#)

Harry Kalodner, Steven Goldfeder, Xiaoqi Chen, S. Matthew Weinberg, and Edward W. Felten, *Princeton University*

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#### [Erays: Reverse Engineering Ethereum's Opaque Smart Contracts](#)

Yi Zhou, Deepak Kumar, Surya Bakshi, Joshua Mason, Andrew Miller, and Michael Bailey, *University of Illinois, Urbana-Champaign*

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# Smart Contract Vulnerabilities: Research

- ACM CCS 2018

## **Smart Contracts** (203 AB)

*Session Chair: Yan Chen*

### **SECURIFY: Practical Security Analysis of Smart Contracts**

*Petar Tsankov (ETH Zurich), Andrei Marian Dan (ETH Zurich), Dana Drachler Cohen (ETH Zurich), Arthur Gervais (Imperial College London), Florian Buenzli (ETH Zurich), Martin Vechev (ETH Zurich)*

### **BitML: a calculus for Bitcoin smart contracts**

*Massimo Bartoletti (University of Cagliari), Roberto Zunino (University of Trento)*



# Vulnerable Semantics of Solidity: Scope

## Scoping and Declarations

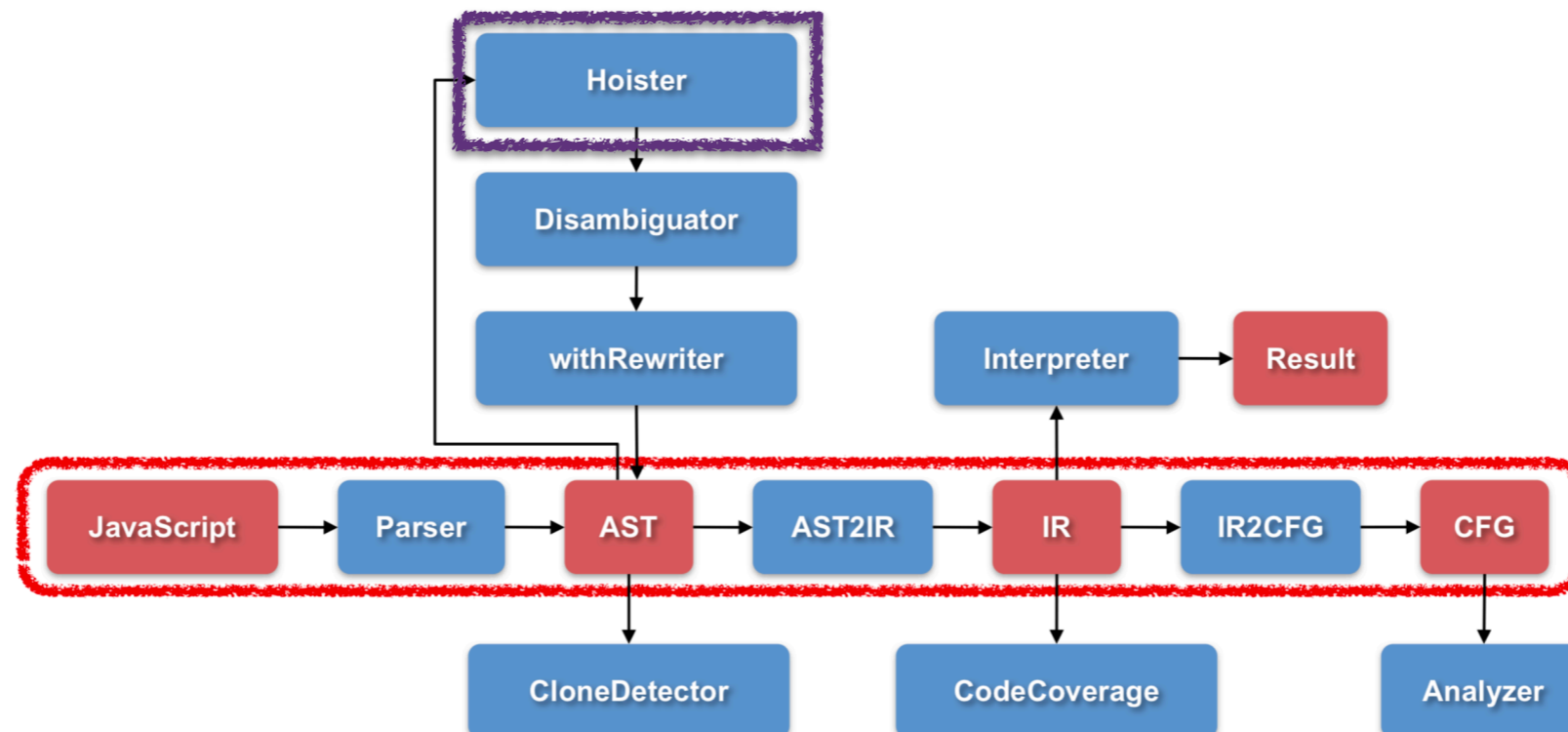
A variable declared anywhere within a function will be in scope for the *entire function*, regardless of where it is declared (this will change soon, see below). This happens because Solidity inherits its scoping rules from JavaScript. This is in contrast to many languages where variables are only scoped where they are declared until the end of the semantic block. As a result, the following code is illegal and cause the compiler to throw an error, `Identifier already declared`:



# Vulnerable Semantics of Solidity: Scope

## Scoping and Declarations

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## Scoping starting from Version 0.5.0

Starting from version 0.5.0, Solidity will change to the more widespread scoping rules of C99 (and many other languages): Variables are visible from the point right after their declaration until the end of a `{ }`-block. As an exception to this rule, variables declared in the initialization part of a for-loop are only visible until the end of the for-loop.

# Vulnerable Semantics of Solidity: MM

## Overload resolution and Argument matching

Overloaded functions are selected by matching the function declarations in the current scope to the arguments supplied in the function call. Functions are selected as overload candidates if all arguments can be implicitly converted to the expected types. If there is not exactly one candidate, resolution fails.

### Note

Return parameters are not taken into account for overload resolution.

```
pragma solidity ^0.4.16;

contract A {
    function f(uint8 _in) public pure returns (uint8 out) {
        out = _in;
    }

    function f(uint256 _in) public pure returns (uint256 out) {
        out = _in;
    }
}
```

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**Return Type Rule:**  $\Delta \vdash d$  return type wrt  $d$  ok

$$\begin{array}{c}
 \frac{\text{name}(d) \neq \text{name}(d')}{\Delta \vdash d \text{ return type wrt } d' \text{ ok}} \quad [\text{RETURN-TRIV}] \qquad \frac{\neg(\Delta \vdash \text{dom}(d) \sqsubseteq \text{dom}(d'))}{\Delta \vdash d \text{ return type wrt } d' \text{ ok}} \quad [\text{RETURN-NOT-LESS}] \\
 \\
 \frac{\text{arrow}(d) = \forall[\bar{\kappa}](\alpha \rightarrow \rho) \quad \overline{\kappa = \{\bar{\chi}\} <: P <: \{\bar{\eta}\}} \quad \text{arrow}(d') = \forall[\bar{\kappa}'](\alpha' \rightarrow \rho')}{\overline{\kappa' = \{\bar{\chi}'\} <: Q <: \{\bar{\eta}'\}} \quad \text{distinct}(\bar{P}, \bar{Q}) \quad \Delta \vdash \text{dom}(d) \sqsubseteq \text{dom}(d')} \\
 \frac{\Delta \vdash \forall[\bar{\kappa}](\alpha \rightarrow \rho) \sqsubseteq \forall[\bar{\kappa}, \bar{\kappa}']((\alpha \sqcap \alpha') \rightarrow \rho')}{\Delta \vdash d \text{ return type wrt } d' \text{ ok}} \quad [\text{RETURN-TEST}]
 \end{array}$$

# Vulnerable Semantics of Solidity: MM

## Multiple Inheritance and Linearization

Languages that allow multiple inheritance have to deal with several problems. One is the [Diamond Problem](#). Solidity is similar to Python in that it uses “[C3 Linearization](#)” to force a specific order in the DAG of base classes. This results in the desirable property of monotonicity but disallows some inheritance graphs. Especially, the order in which the base classes are given in the `is` directive is important: You have to list the direct base contracts in the order from “most base-like” to “most derived”. Note that this order is different from the one used in Python. In the following code, Solidity will give the error “Linearization of inheritance graph impossible”.

```
// This will not compile  
  
pragma solidity ^0.4.0;  
  
contract X {}  
contract A is X {}  
contract C is A, X {}
```

The reason for this is that `C` requests `X` to override `A` (by specifying `A, X` in this order), but `A` itself requests to override `X`, which is a contradiction that cannot be resolved.

# Vulnerable Semantics of Solidity: MM

```
pragma solidity ^0.4.22;
```

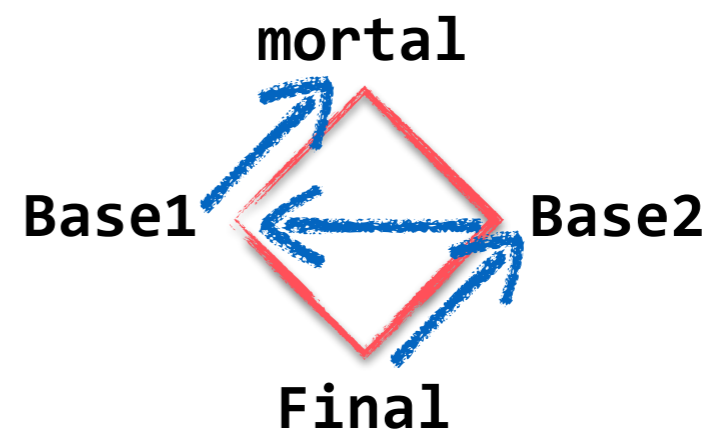
```
contract owned { ... }
```

```
contract mortal is owned {  
    function kill() public {  
        if (msg.sender == owner) selfdestruct(owner);  
    }  
}
```

```
contract Base1 is mortal {  
    function kill() public { /* cleanup 1 */ mortal.kill(); }  
}
```

```
contract Base2 is mortal {  
    function kill() public { /* cleanup 2 */ mortal.kill(); }  
}
```

```
contract Final is Base1, Base2 { ... }
```



# Vulnerable Semantics of Solidity: MM

```
pragma solidity ^0.4.22;
```

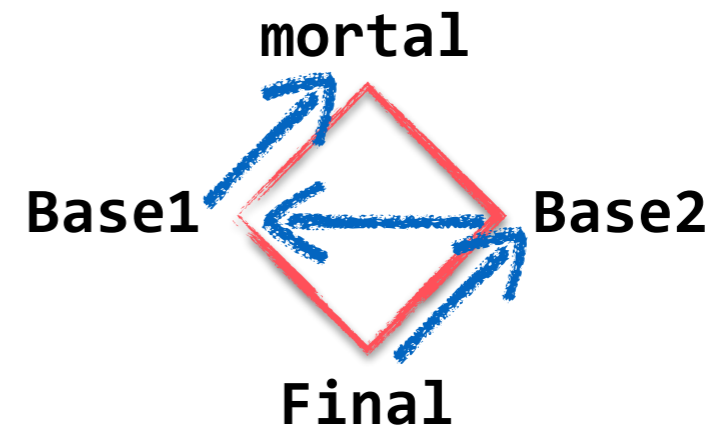
```
contract owned { ... }
```

```
contract mortal is owned {  
    function kill() public {  
        if (msg.sender == owner) selfdestruct(owner);  
    }  
}
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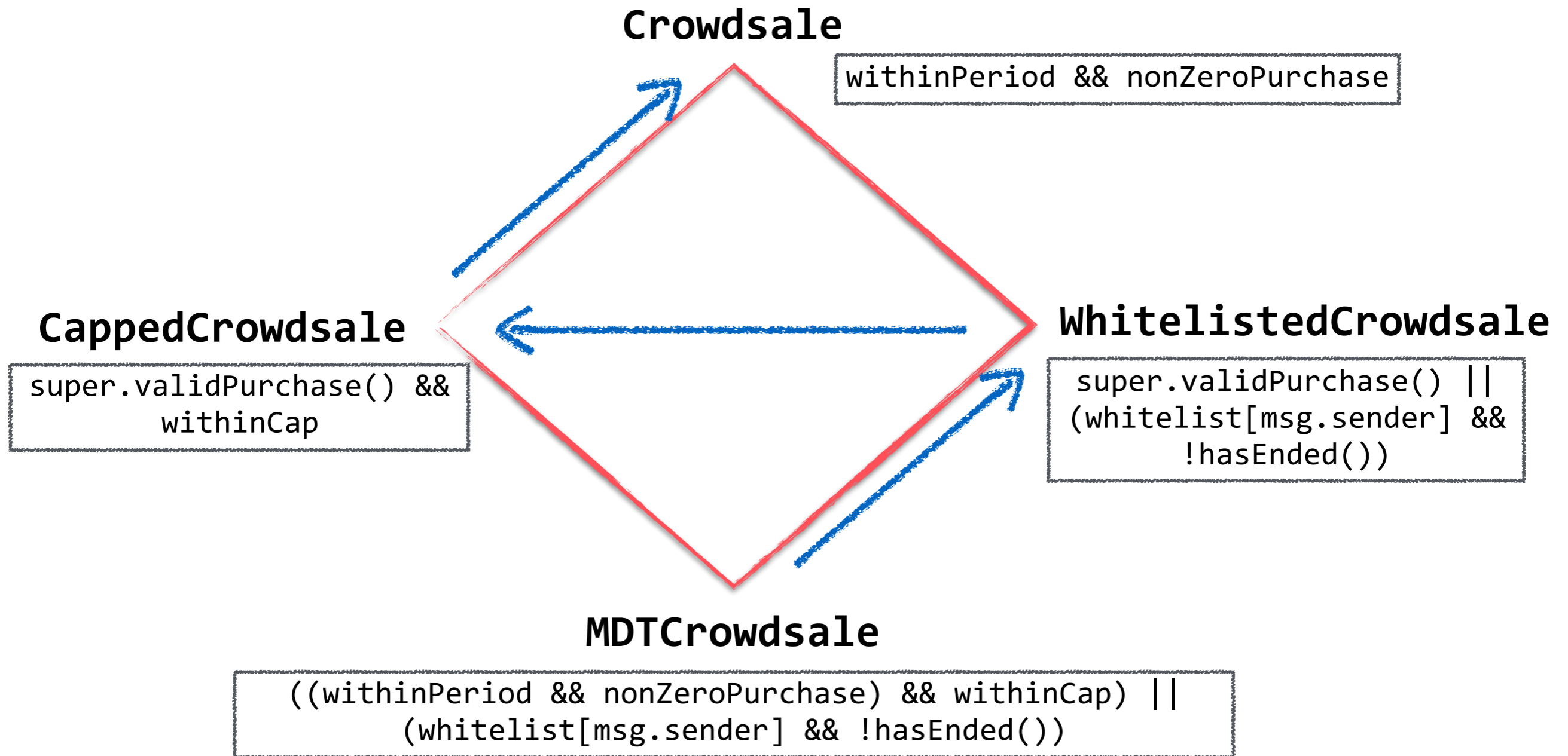
```
contract Base1 is mortal {  
    function kill() public { /* cleanup 1 */ super.kill(); }  
}
```

```
contract Base2 is mortal {  
    function kill() public { /* cleanup 2 */ super.kill(); }  
}
```

```
contract Final is Base1, Base2 { ... }
```



# Vulnerable Semantics of Solidity: MM



<https://pdaian.com/blog/solidity-anti-patterns-fun-with-inheritance-dag-abuse/>



# Vulnerable Semantics of Solidity: MM

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(The name "C3" is not an [initialism](#).) It was first published at the 1996 [OOPSLA](#) conference, in a paper entitled "[A Monotonic Superclass Linearization for Dylan](#)".<sup>[1]</sup> It was adapted to the Open Dylan implementation in January 2012<sup>[2]</sup> following an enhancement proposal.<sup>[3]</sup> It has been chosen as the default algorithm for method resolution in [Python 2.3](#) (and newer),<sup>[4][5]</sup> [Perl 6](#),<sup>[6]</sup> [Parrot](#),<sup>[7]</sup> [Solidity](#), and [PGF/TikZ's Object-Oriented Programming module](#)<sup>[8]</sup>. It is also available as an alternative, non-default MRO in the core of [Perl 5](#) starting with version 5.10.0.<sup>[9]</sup> An extension implementation for earlier versions of Perl 5 named `Class::C3` exists on [CPAN](#).<sup>[10]</sup>

# Smart Contract Vulnerabilities: Research

- Which platform?
  - ◆ Ethereum, Michelson/Liquidity, Zilliqa/Scilla, ...
- Which language?
  - ◆ Source-level: Solidity, LLL, Vyper, ...
  - ◆ Bytecode
- What problems?
  - ◆ Bugs: type-related, resource-related, ...
  - ◆ Vulnerabilities: security, privacy, ...

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- PL to save the world from *bugs* in real-world applications
- PL with *proofs*
- PL for **Software Engineering**
- PL for **Security**
- **열심히, 즐겁게, 자발적으로**



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