Learning Certified Individually Fair Representations

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Fair Representation Learning

We consider individual fairness, which requires that similar individuals should be treated similarly. More concretely, we focus on individual fairness in the following context [McNamara et al., 2019]:

- **Data Regulator**: defines fairness notion for the task
- **Data Producer**: transforms user data into latent representation
- **Data Consumer**: performs predictions based on latent representation
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**Key Challenge:** enforce individual fairness in the setting described above by learning and certifying individually fair representations
Data Regulator

We propose an individual fairness notion in terms of interpretable logical constraints. For example, for an individual $x \in R^N$ we want all similar individuals, defined as $x' \in R^N$ such that

$$\phi(x, x') := \bigwedge_{i \in \text{Categorical} \setminus \{\text{race, gender}\}} (x_i = x'_i) \bigwedge_{j \in \text{Numerical}} |x_j - x'_j| \leq \alpha,$$

to be classified the same.
Individual Fairness

We define $S_\phi(x) := \{x' \in R^N \mid \phi(x, x')\}$ to be the set of all individuals similar to $x$. We want to certify for individual $x$ in the test dataset,

$$\forall x' \in S_\phi(x) \Rightarrow \mu(M(x), M(x')),$$

where $M : R^N \rightarrow R^O$ is the model, and $\phi : R^N \times R^N \rightarrow \{0, 1\}$ and $\mu : R^O \times R^O \rightarrow \{0, 1\}$ are binary similarity measures on inputs and outputs.

We consider classification with $\mu(M(x), M(x')) \iff M(x) = M(x')$. 
Data Producer

• trains encoder $f_\theta : R^N \rightarrow R^K$, where $K$ is the dimension of the latent space, such that $\forall x' \in S_\phi(x) \Rightarrow |f_\theta(x) - f_\theta(x')|_\infty \leq \delta$

• encodes $S_\phi(x)$ and $f_\theta$ as mixed-integer linear program (MILP) to compute $\epsilon$ such that $f_\theta(S_\theta(X)) \subseteq \{z' ||z - z'|_\infty \leq \epsilon\}$ for $z := f_\theta(x)$
Data Consumer

• obtains $z$ and $\epsilon$ from data producer and uses standard local robustness training to obtain a classifier $h_\psi : \mathbb{R}^K \rightarrow \mathbb{R}^O$ that is robust to $l_\infty$-perturbations of magnitude $\epsilon$ around $z$

• uses neural network robustness verifier to certify $\epsilon$-robustness for $z$
Experimental Evaluation

\[ \phi(x, x') := \bigwedge_{i \in \text{Categorical} \setminus \{\text{race, gender}\}} (x_i = x_i') \bigwedge_{j \in \text{Numerical}} |x_j - x_j'| \leq \alpha, \]

<table>
<thead>
<tr>
<th>Dataset</th>
<th>Accuracy (%)</th>
<th>Certified Individual Fairness (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Baseline</td>
<td>LCIFR</td>
</tr>
<tr>
<td>Adult</td>
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<td>81.3</td>
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<tr>
<td>Compas</td>
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<tr>
<td>Crime</td>
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<tr>
<td>Health</td>
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<td>80.7</td>
</tr>
<tr>
<td>Law School</td>
<td>84.4</td>
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</tr>
</tbody>
</table>

Learning certified individually fair representations (LCIFR) significantly increases the percentage of points with certified individual fairness, without compromising accuracy.
Conclusion

\[ \phi(x, x') := \bigwedge_{i \in \text{Categorical} \setminus \{\text{race, gender}\}} (x_i = x'_i) \bigwedge_{j \in \text{Numerical}} |x_j - x'_j| \leq \alpha, \]

Code: [https://github.com/eth-sri/lcifr](https://github.com/eth-sri/lcifr)